

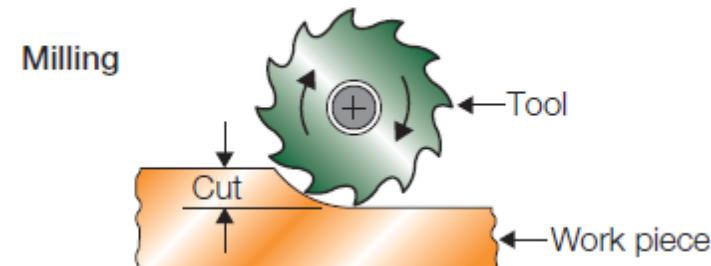
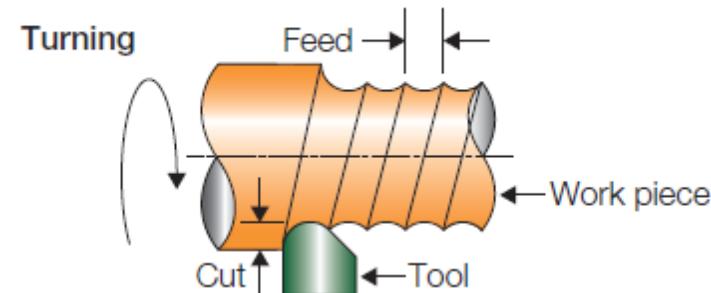
# **Lecture 6 - 'Classical machining' / material removal through mechanical means**

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**EPFL**

# Learning objectives

1. Methods related to **material removal by mechanical means** involving cutting techniques ('*Enlèvements de copeaux*')
  1. **Cutting** ('*Découpe*')
  2. **Milling** ('*Fraisage*')
  3. **Drilling** ('*Perçage*')
  4. **Turning** ('*Tournage*')
2. Differences between processes like
3. Modelling



(Illustration M. Ashby)

# Machining through material removal processes

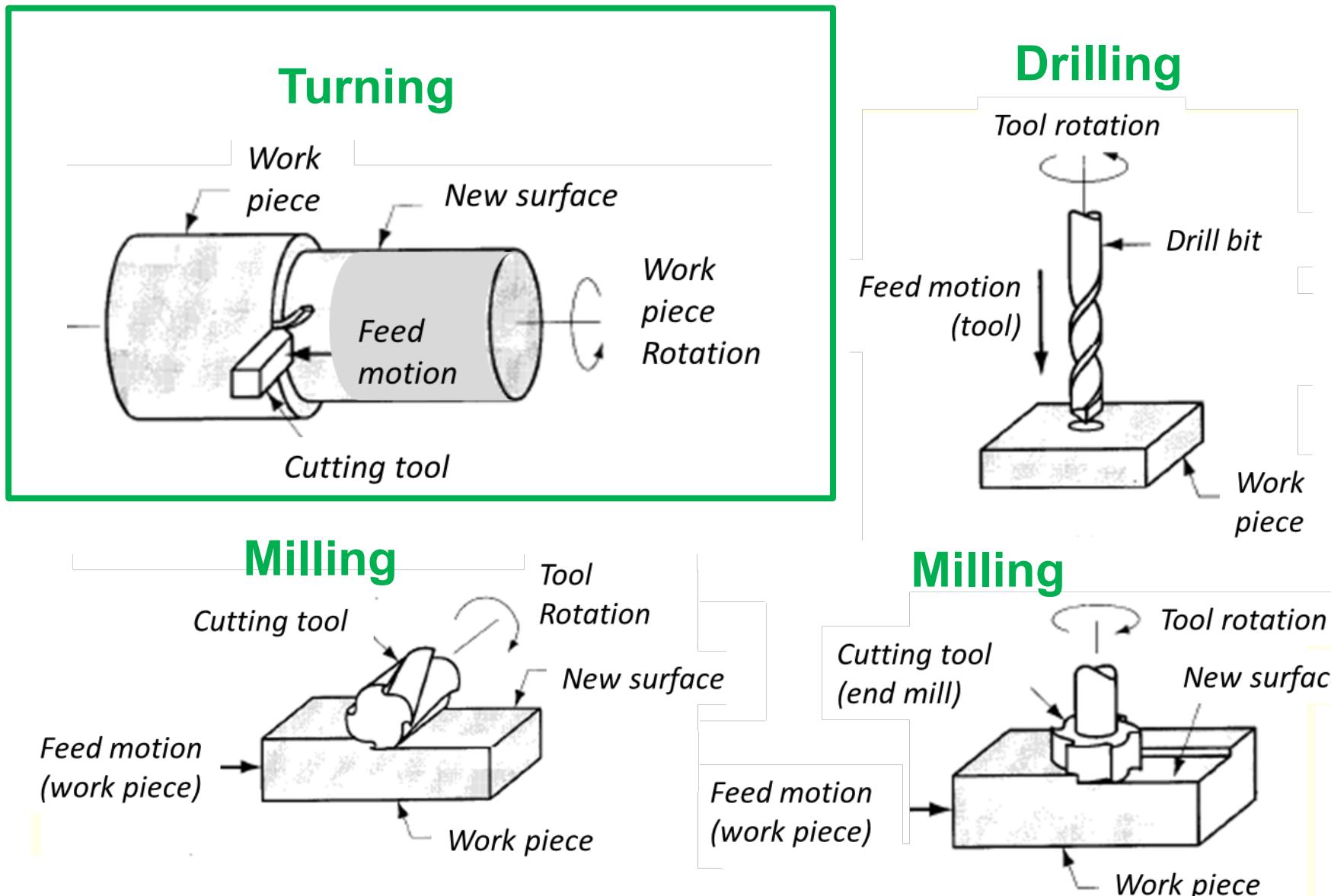
**'Removal** of material from a raw material so the remaining material has the desired, final shape'

- *Machining* – material removal by a sharp cutting tool (turning, milling, drilling)
- *Abrasion* – material removal by hard, abrasive particles (grinding, lapping, polishing)
- *Unconventional* – lasers, *EDM*, water-jet etc.

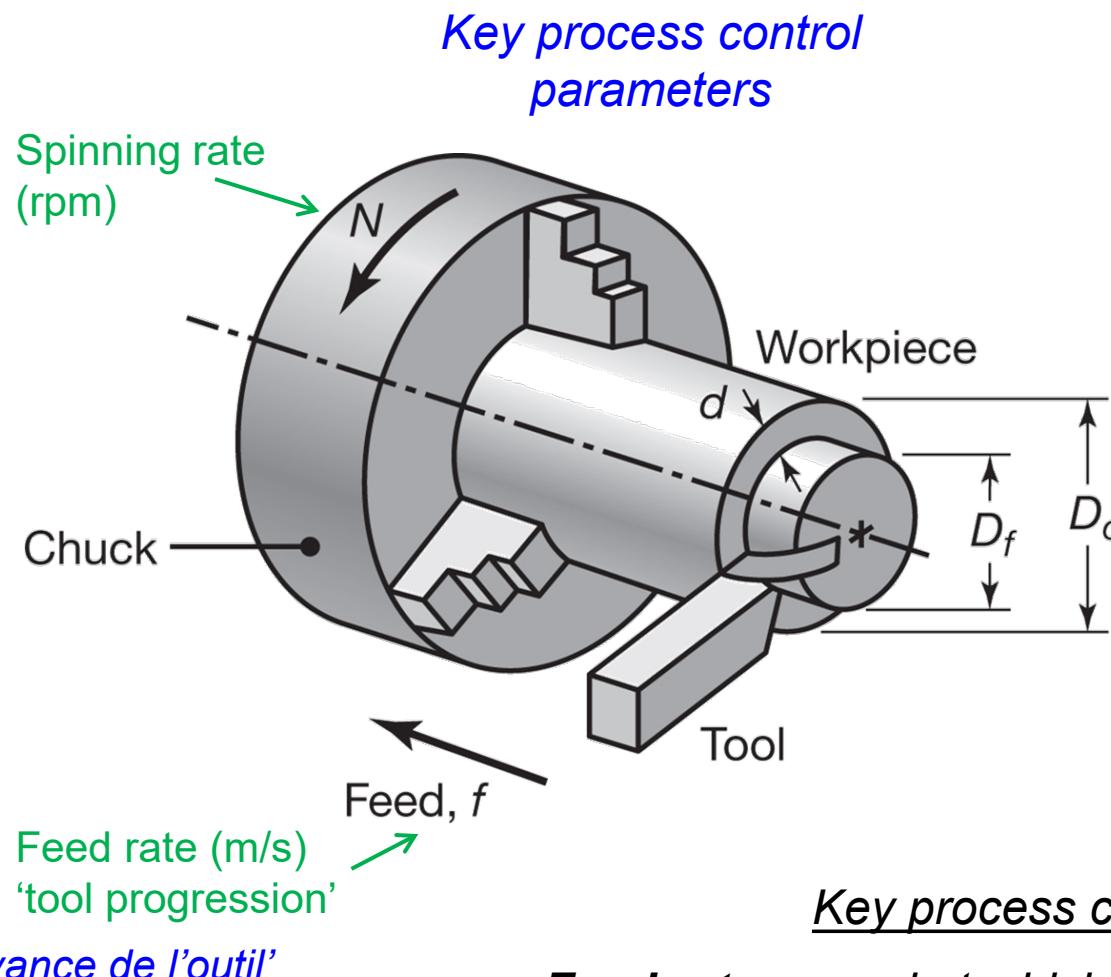
# Why Machining is Important...

- **Variety of work materials** can be machined
  - Most frequently applied to metals (but not only!)
- **Variety of part shapes and special geometry features:**
  - Threads (screw)
  - Accurate round holes
  - Straight edges and surfaces
- 0.01 mm to micron dimensional accuracy and surface finish (down to optical quality – in the case of diamond turning)

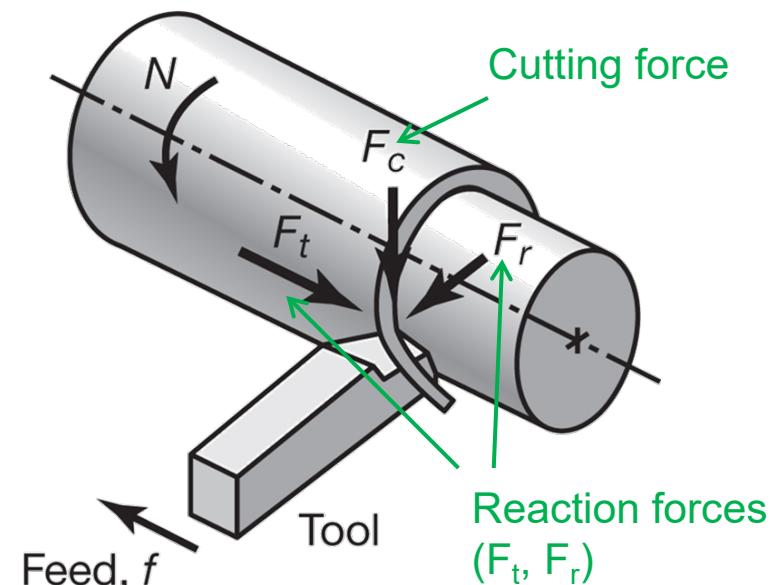
# Metal cutting operations



# Metal cutting operations: turning



*Force acting on a cutting tool during operation*



Key process control parameters:

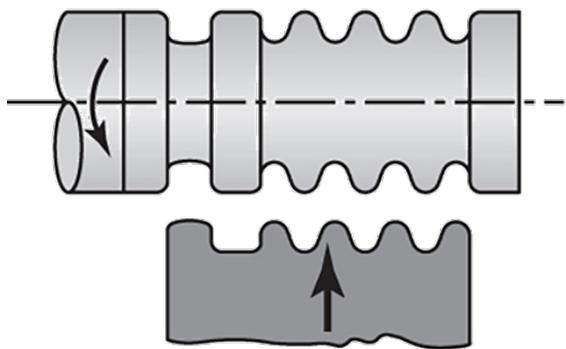
- **Feed rate:** speed at which the tools move into the specimen
- **Spinning rate (N):** rotational speed of the tool

# Illustrative video

<https://youtu.be/8EsAxOnzEms>

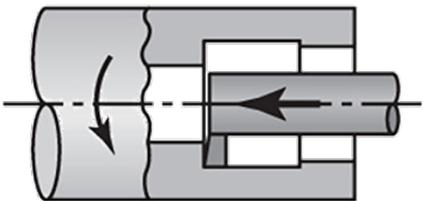
# Turning terminology

*'Découpe avec outil de forme'*



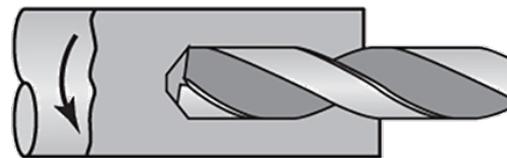
(g) Cutting with a form tool

*'Alésage'*



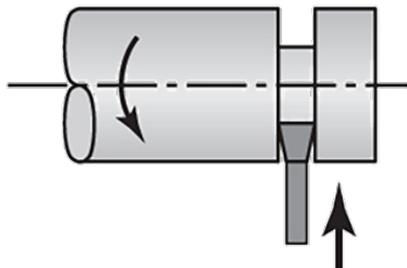
(h) Boring and internal grooving

*'Perçage'*



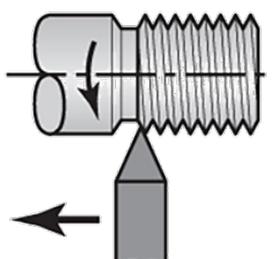
(i) Drilling

*'Découpe'*



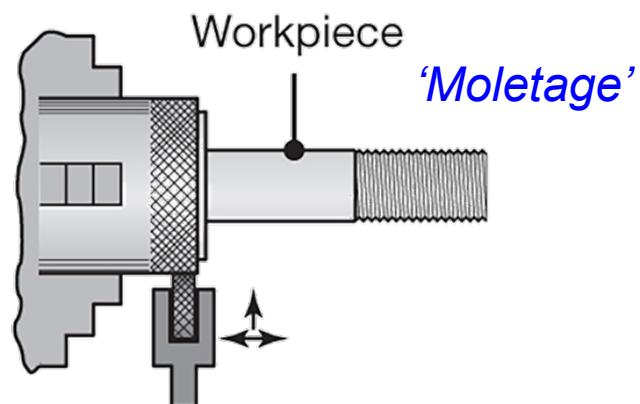
(j) Cutting off

*'Taraudage'*



(k) Threading

Workpiece

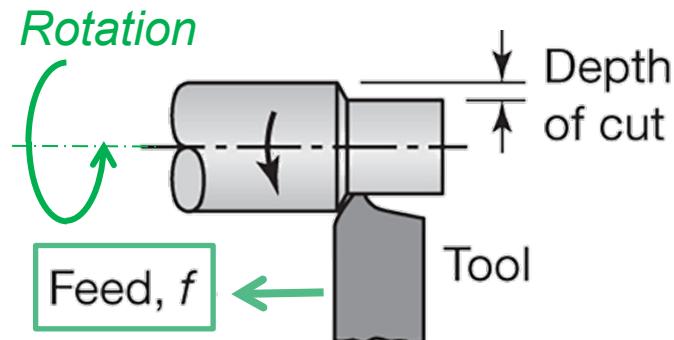


*'Moletage'*

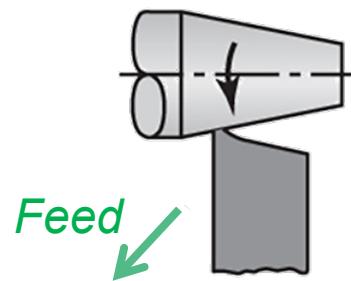
(l) Knurling

# Turning

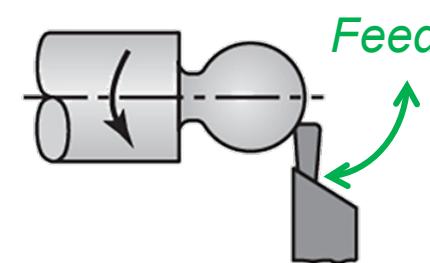
*Different shape are obtained by proper choice of the tool and coordinated motion of the tool.*



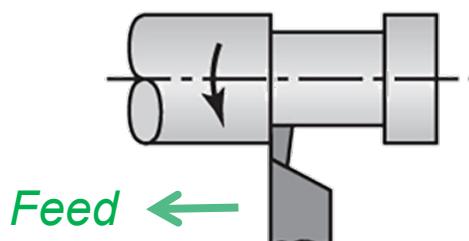
(a) Straight turning



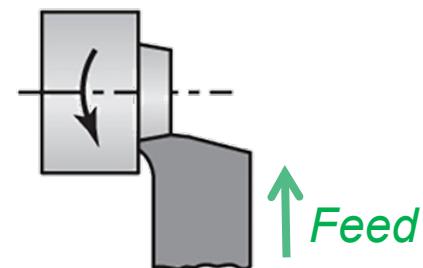
(b) Taper turning



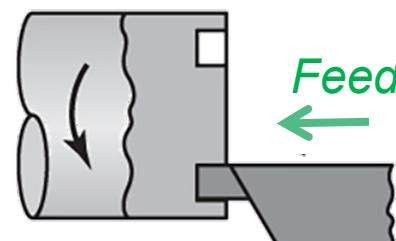
(c) Profiling



(d) Turning and external grooving



(e) Facing



(f) Face grooving

# Illustration of the diversity of tools in watch making



Illustration Polymedia.ch



Illustration Willemin-Macodel



(Source: Louis Bélet, Swiss cutting tool)

# Precision Turning ('Decolletage')

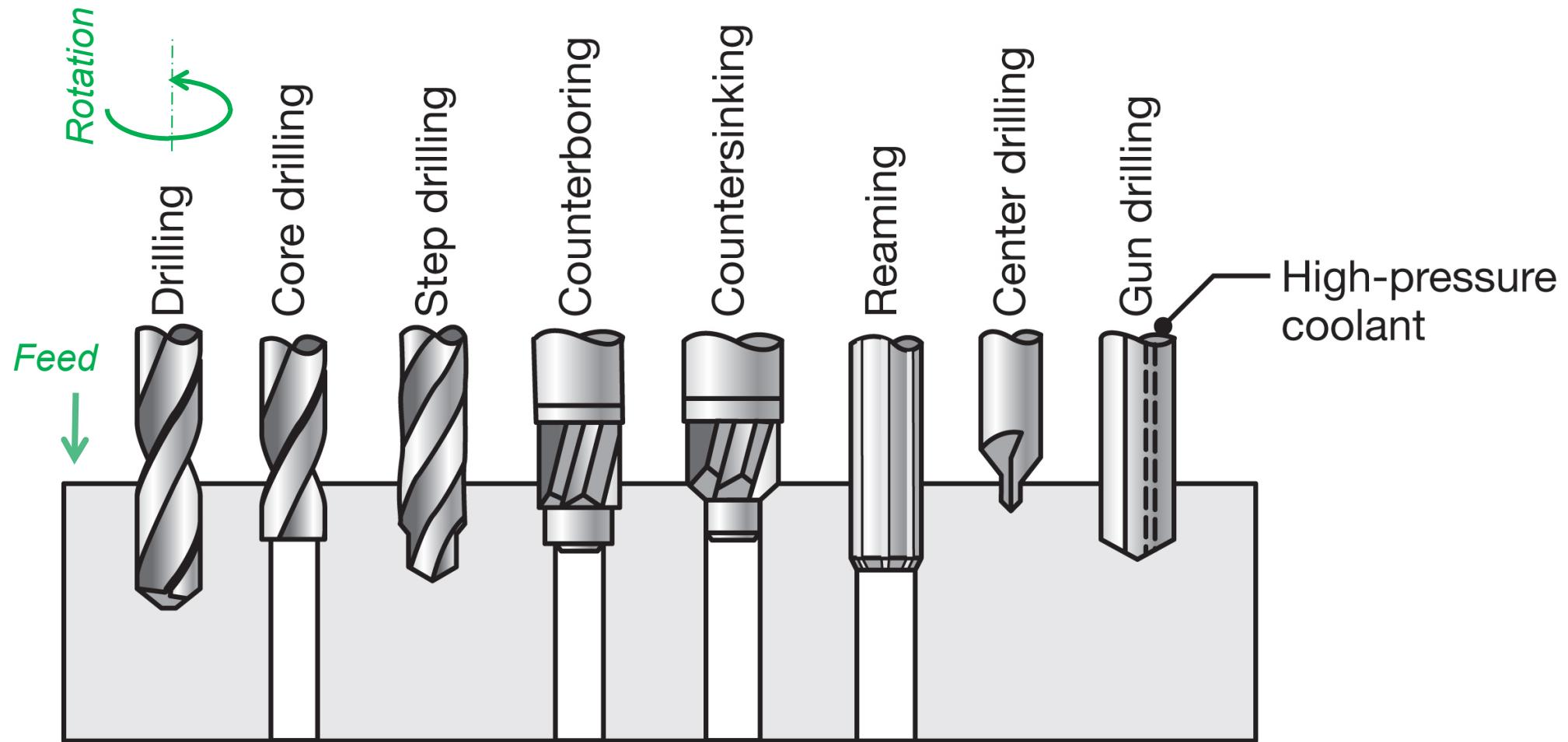


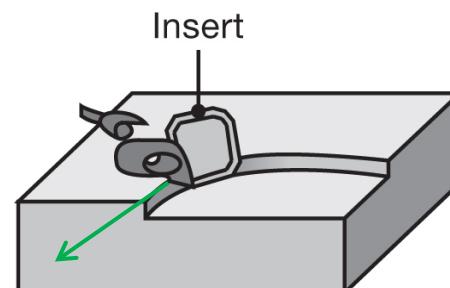
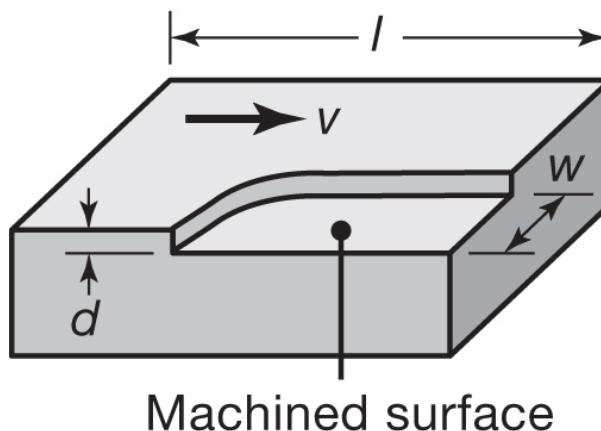
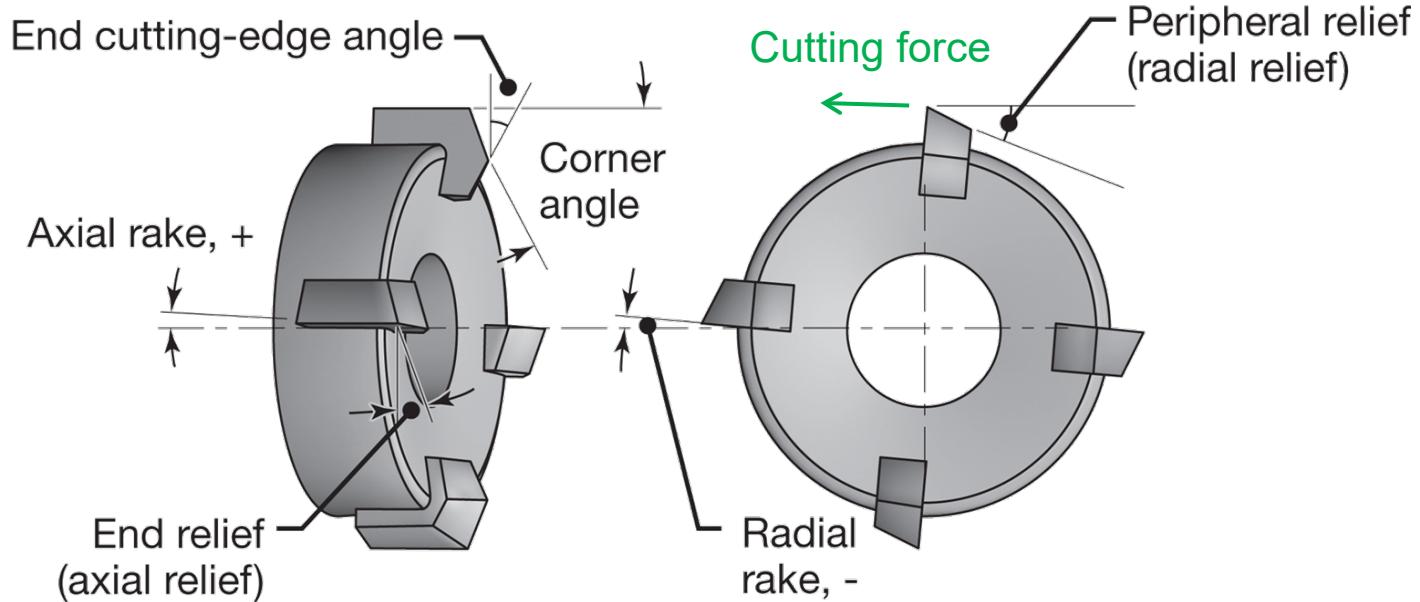
(source Snaem)

(source: 3D Décolletage)

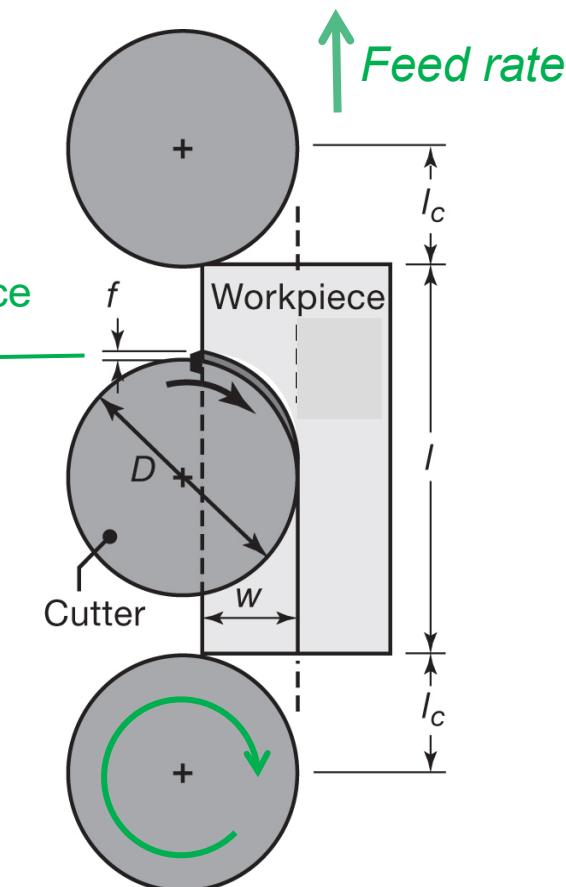


# Drilling operations





*Spinning rate (N)*



## Face milling 'Fraisage'

# Typical manufacturing Sequence



1. Raw material is prepared by **forming processes**, such as casting, forging, rolling and bar drawing
2. **Machining provides the final shape**, dimensions, finish, and special geometric details that other processes cannot create
3. May be followed by **additional finishing steps** (for instance anodizing and other surface treatments)

(ex. Rollomatic)

# Machine Tools

- Modern machine centers are complex machines (= robots)
- Functions:
  - Holds the work piece
  - Positions tool relative to work
  - Provides power at speed, feed, and depth that have been set (CNC controlled)



Illustrative videos:

<https://youtu.be/CqePrbeAQoM>

## Some more videos resources... (for after-class viewing)

- Interesting video showing the variety of machining types:
  - <https://youtu.be/8H-0II7kxbg>
- ‘Miniature’ metal cutting: (Delta robot)
  - <https://youtu.be/As4Qc6Q7H88>
- Machining center (5 axis) (example)
  - [https://youtu.be/7frY\\_qc3-cg](https://youtu.be/7frY_qc3-cg)
- One more thing... <https://youtu.be/sxbilpXZfG8>
- Illustration of machining (watchmakers)
  - <https://www.youtube.com/watch?v=UvCp6DdA1II>
- Optics and diamond turning
  - <https://youtu.be/rJ8U5kwCZDk>

# Advantages

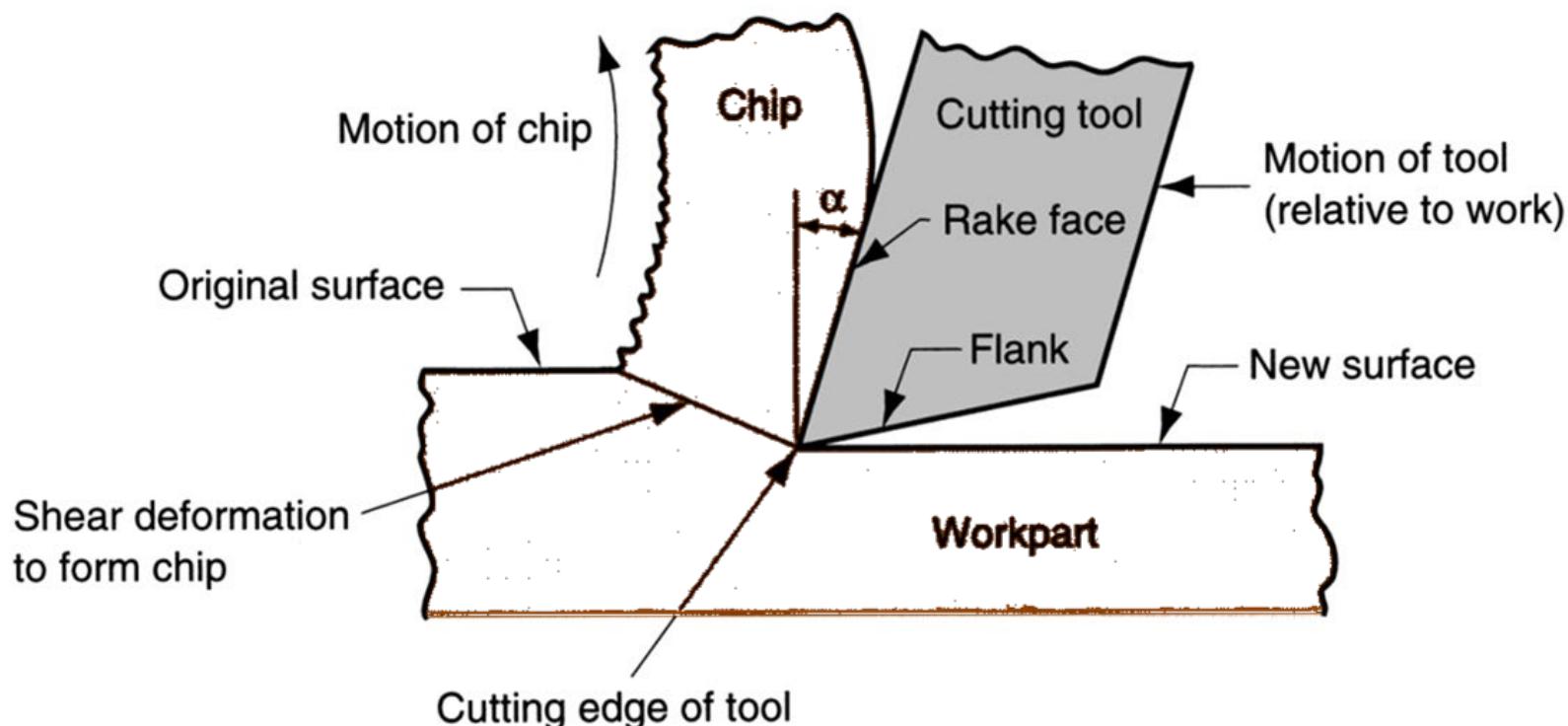
- **High flexibility / 3D**
  - The same machine can make diverse parts with complex features such as threads.
  - Thanks to the progress made in robotics and machine centers, true 3D parts can be made
- **Variety of materials**
  - A broad variety of metals
  - Some polymers (POM for instance)
  - Some brittle materials

# Disadvantages

- **Waste of material / Tooling**
  - Chips generated in machining are wasted material (There are some ongoing attempts to valorize this wasted material, but it cannot be reused for processing)
  - Requires some tooling and cutting fluids for cooling.
- **Time consuming**
  - A machining operation generally takes more time to shape a given part than alternative shaping processes, such as casting, powder metallurgy, or forming
  - Serial operation

# Fundamental working principle

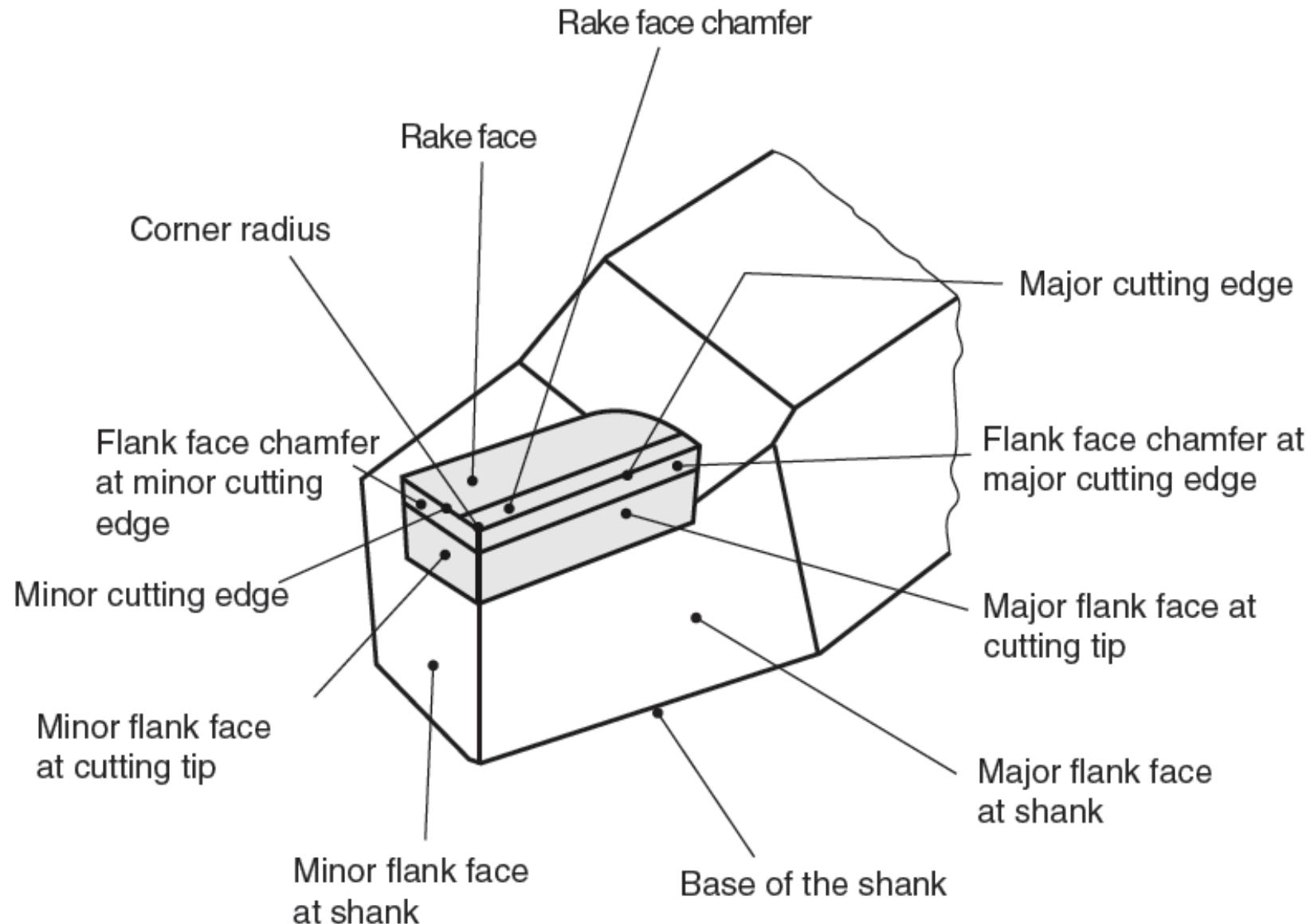
Cutting action involves **shear deformation** of layer of the work material.  
As chip is removed, a new surface is exposed.



# Cutting tools in real life...



# Standardized form of a cutting tool



# Cutting Tool Classification

## 1. Single-Point Tools

- One cutting edge
- **Turning** uses single point tools
- Point is usually rounded to form a *nose radius*



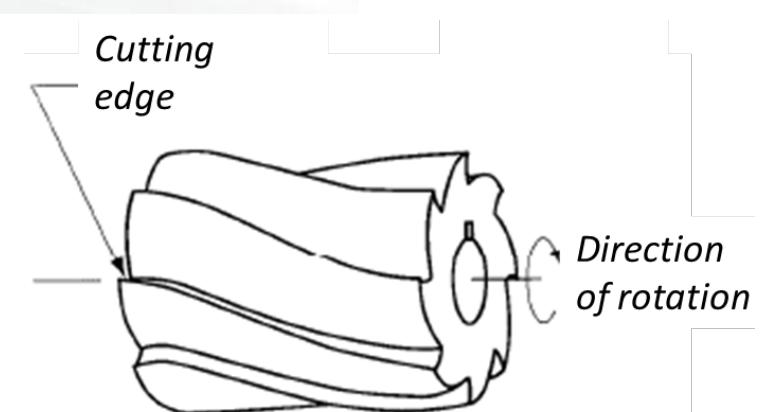
(Source: CNC Blogspot)

## 2. Multiple Cutting Edge Tools

- More than one cutting edge
- Motion relative to work usually achieved by rotating
- **Drilling** and **milling** use rotating multiple cutting edge tools.



(Source: Louis Bélet SA)



# Mechanical analysis of the cutting process: **Why** and **Goals**

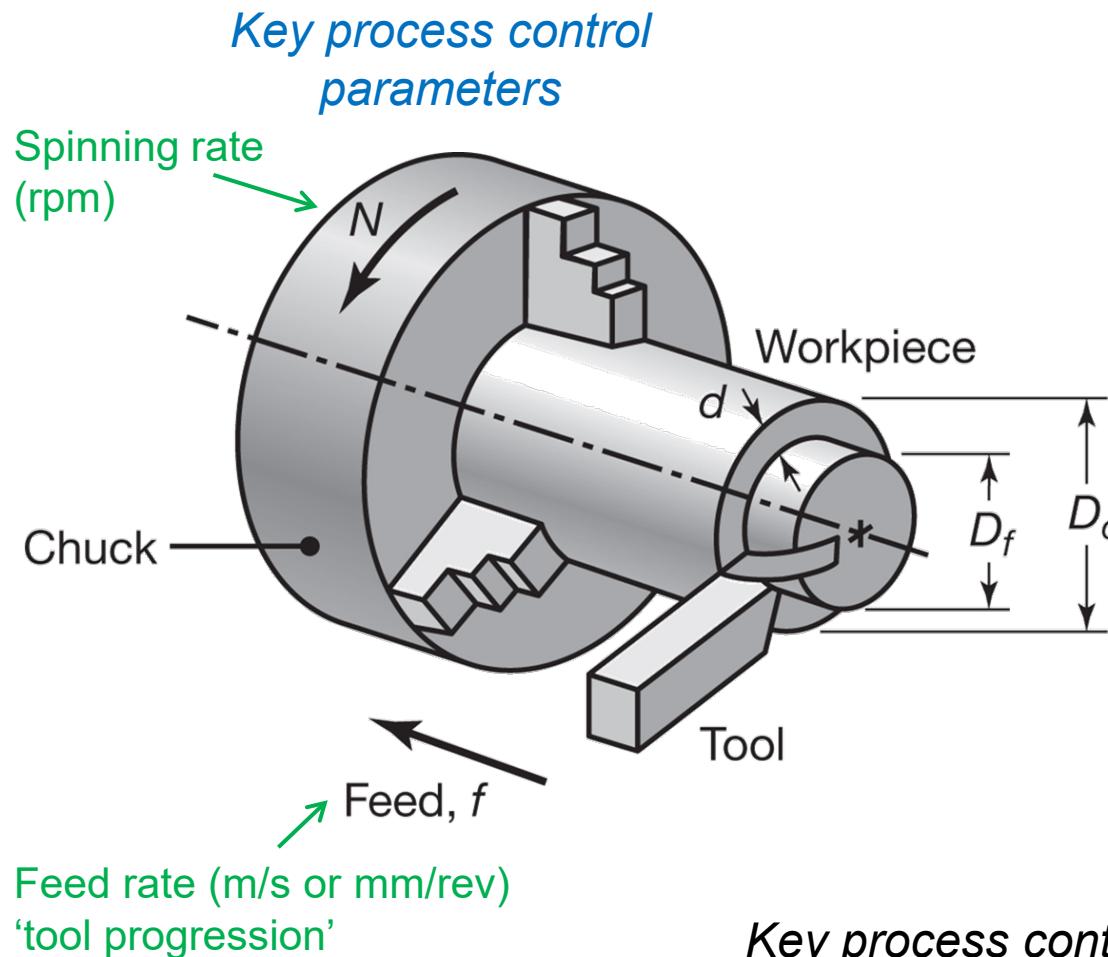
- **Why?**

- Optimize the cutting process in term of tool wear vs material removal rate / increase productivity

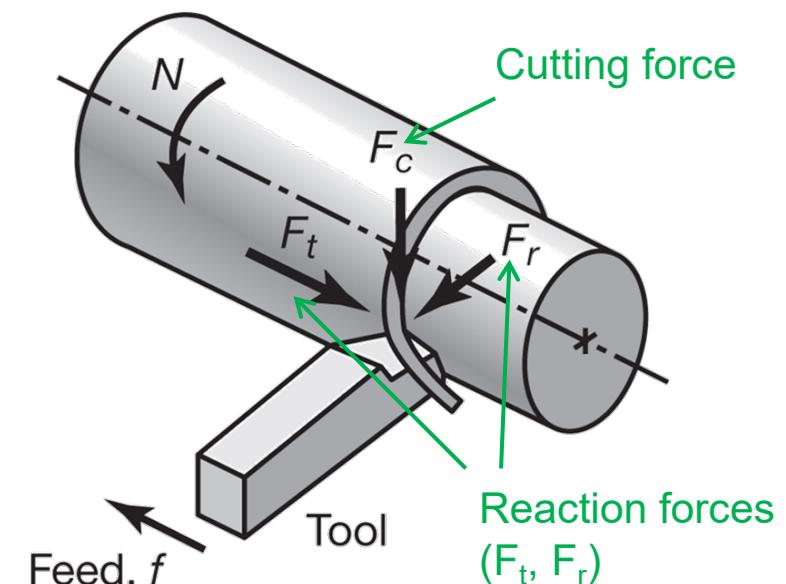
- **Goals**

- Established the force required
  - The power consumption
  - Heat transfer process

# Metal cutting operations: turning



*Force acting on a cutting tool during operation*



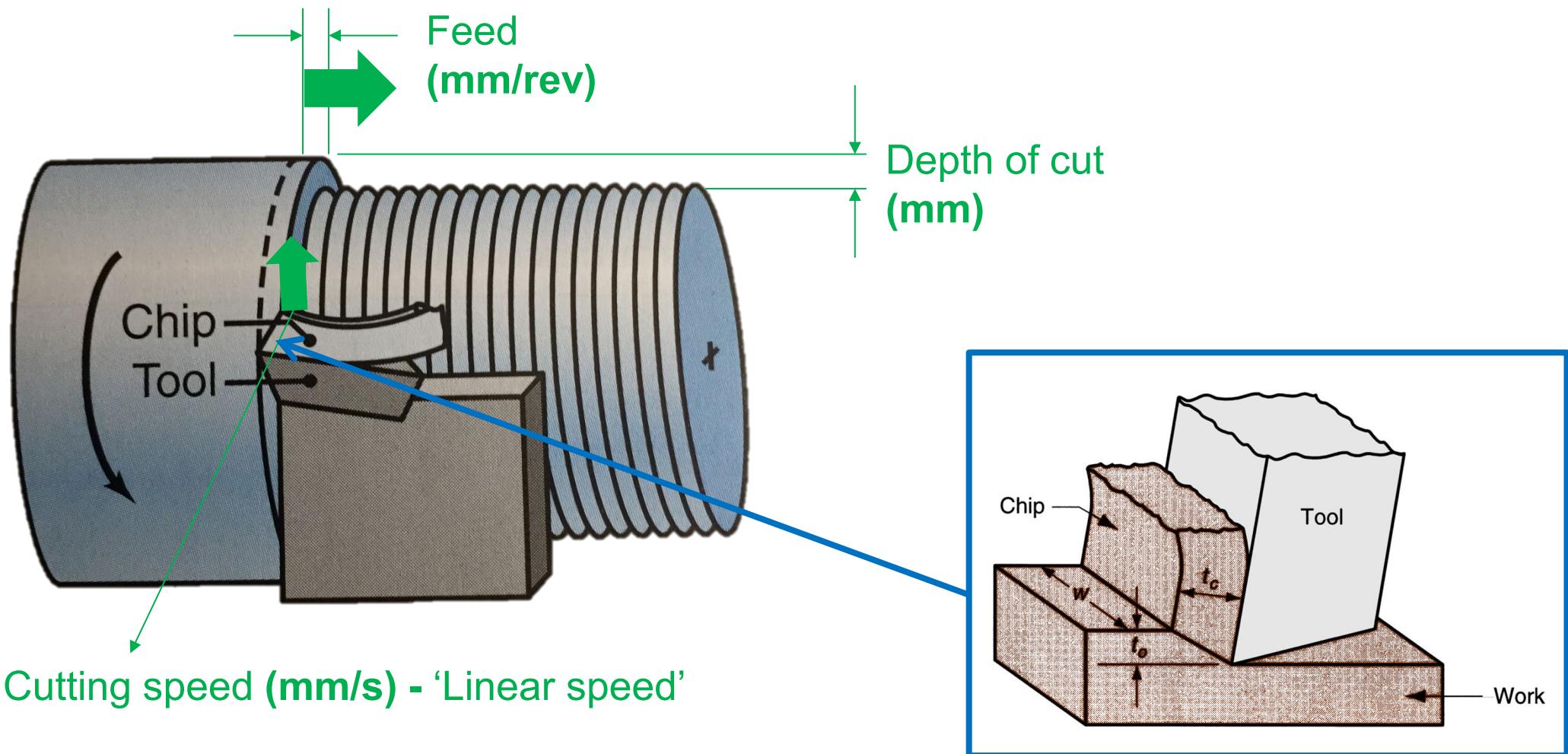
Key process control parameters:

- **Feed rate:** speed at which the tools move into the specimen
- **Spinning rate ( $N$ ):** rotational speed of the tool

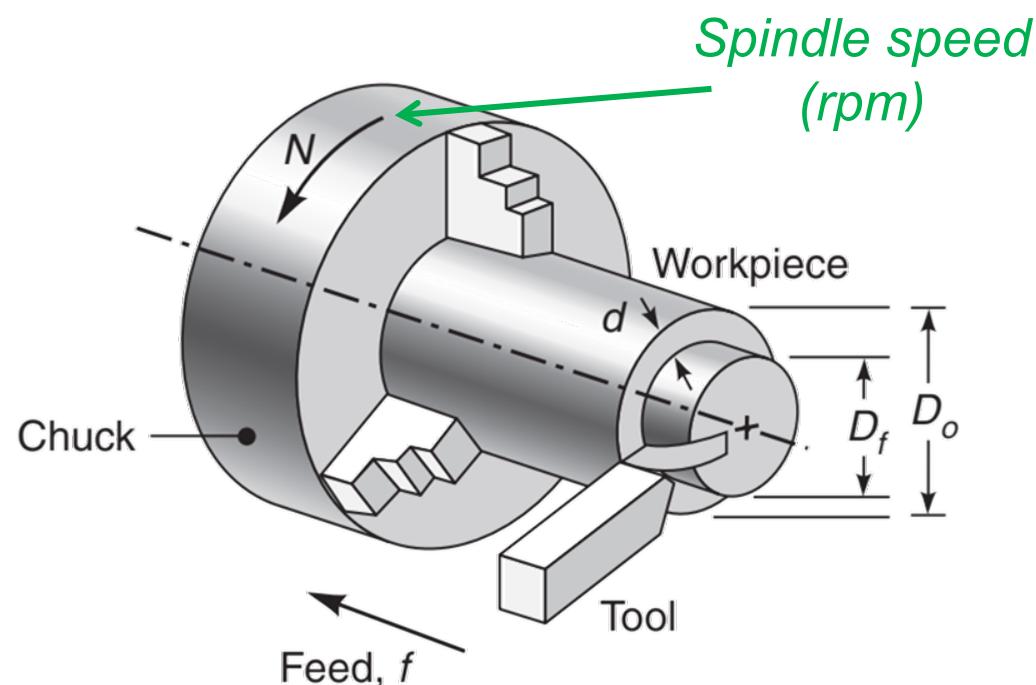
# Some general and tool design parameters influencing machining...

- **Cutting speed, depth of cut, feed, cutting fluids**
  - *Forces, power, temperature rise, tool life, type of chip, surface finish...*
- **Tool angles**
  - *Efficiency, tool resistance*
- **Continuous chip**
  - *Surface finish (but may be undesirable in automated machinery / use of 'chip cutter')*
- **Discontinuous chip**
  - *Fluctuating cutting force, poor surface finish / vibration...*
- **Tool wear**
  - *Surface finish, temperature rise, accuracy*

# Cutting terms



# Material Removal Rate (MRR)



- Average removal rate per revolution:

*Penetration thickness  
of the tool (mm)*

$$\text{Mat}_{/\text{rev}} = d \left[ \pi \left( \frac{D_f + D_o}{2} \right) \right] f$$

*Feed rate mm/rev*

*Average circumference*

- Material removal rate (turning operation)

$$\text{MRR}_{\text{turning}} = \text{Mat}_{/\text{rev}} \times N \quad \text{and}$$

$$\text{mm}^3/\text{min} \longrightarrow \boxed{\text{MRR}_{\text{turning}} = f \times d \times V_{\text{cutting}}}$$

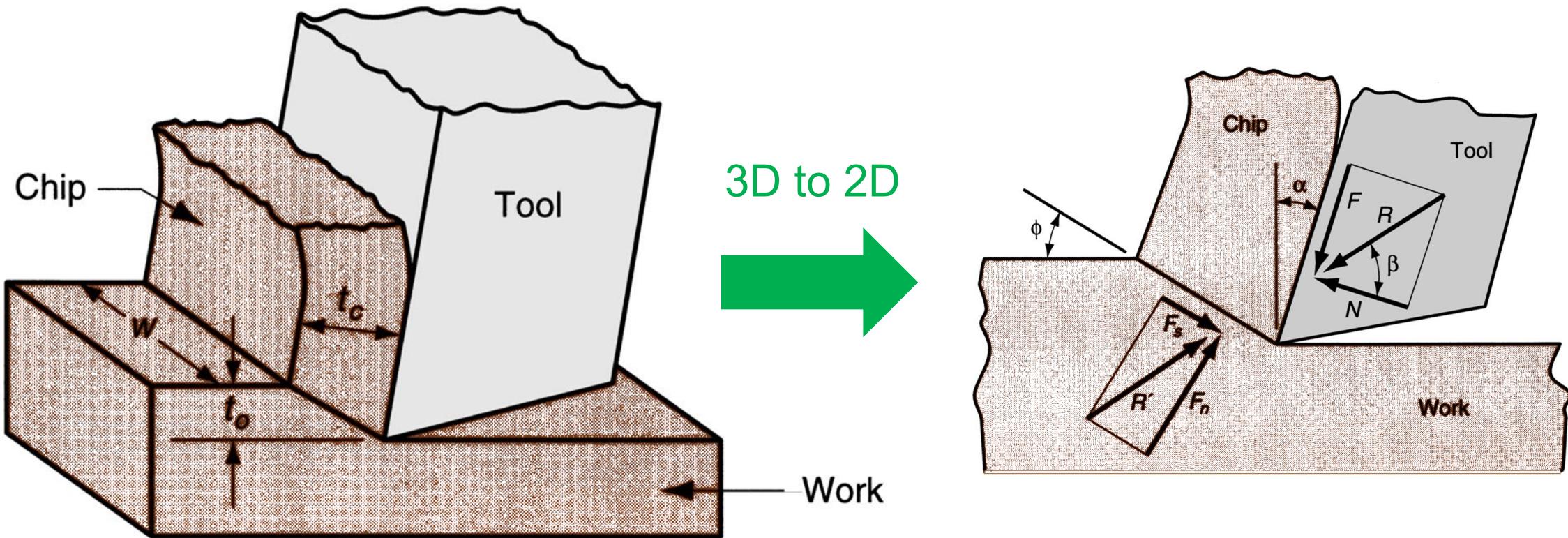
*Average tangential speed  
(mm/min)*

*Spindle speed  
(rpm)*

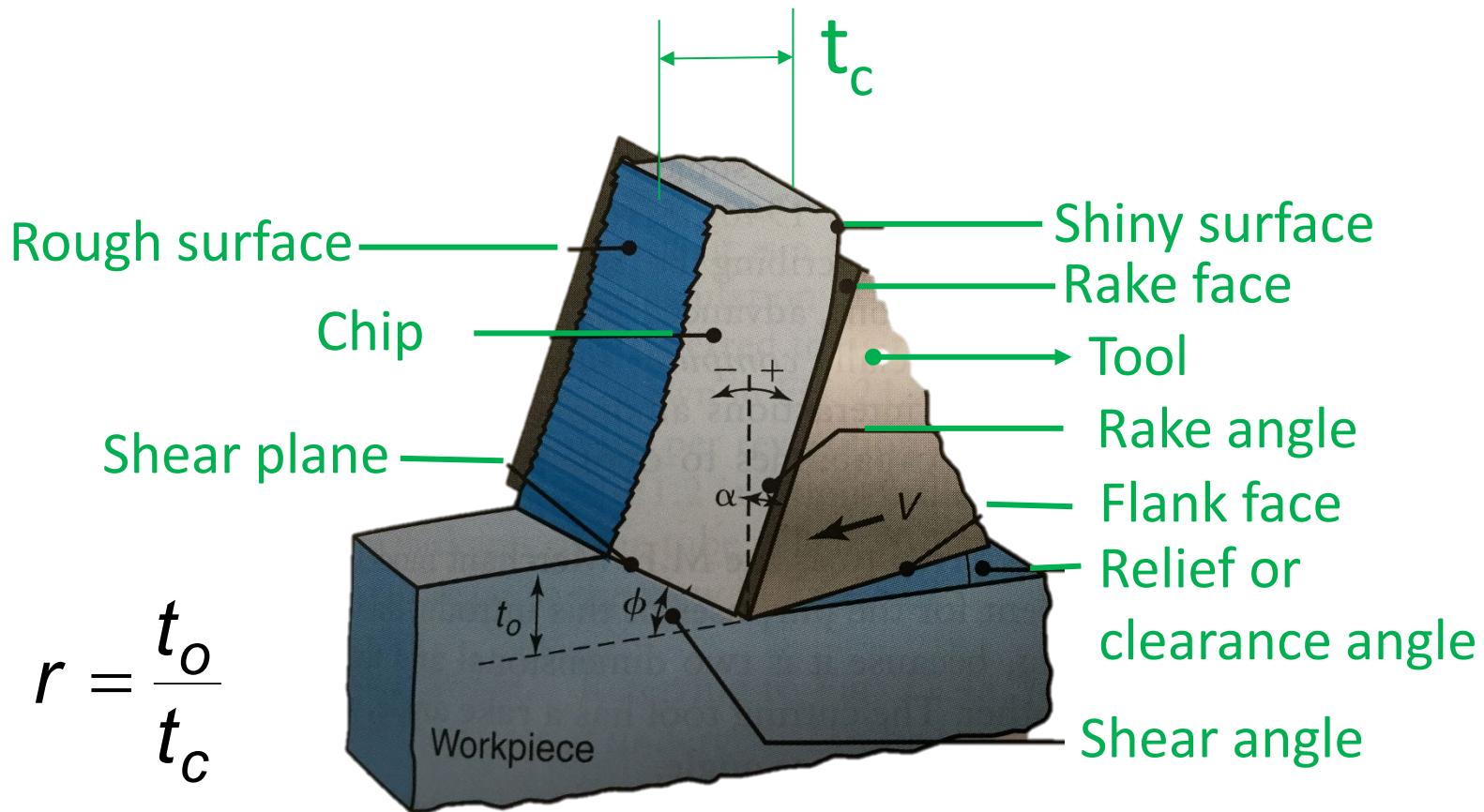
$$V_{\text{cutting}} = \pi \left( \frac{D_f + D_o}{2} \right) N$$

# Modelling... From 3D to 2D (model reduction)

A simplified 2-D model of machining that describes the mechanics of machining with a fair accuracy.



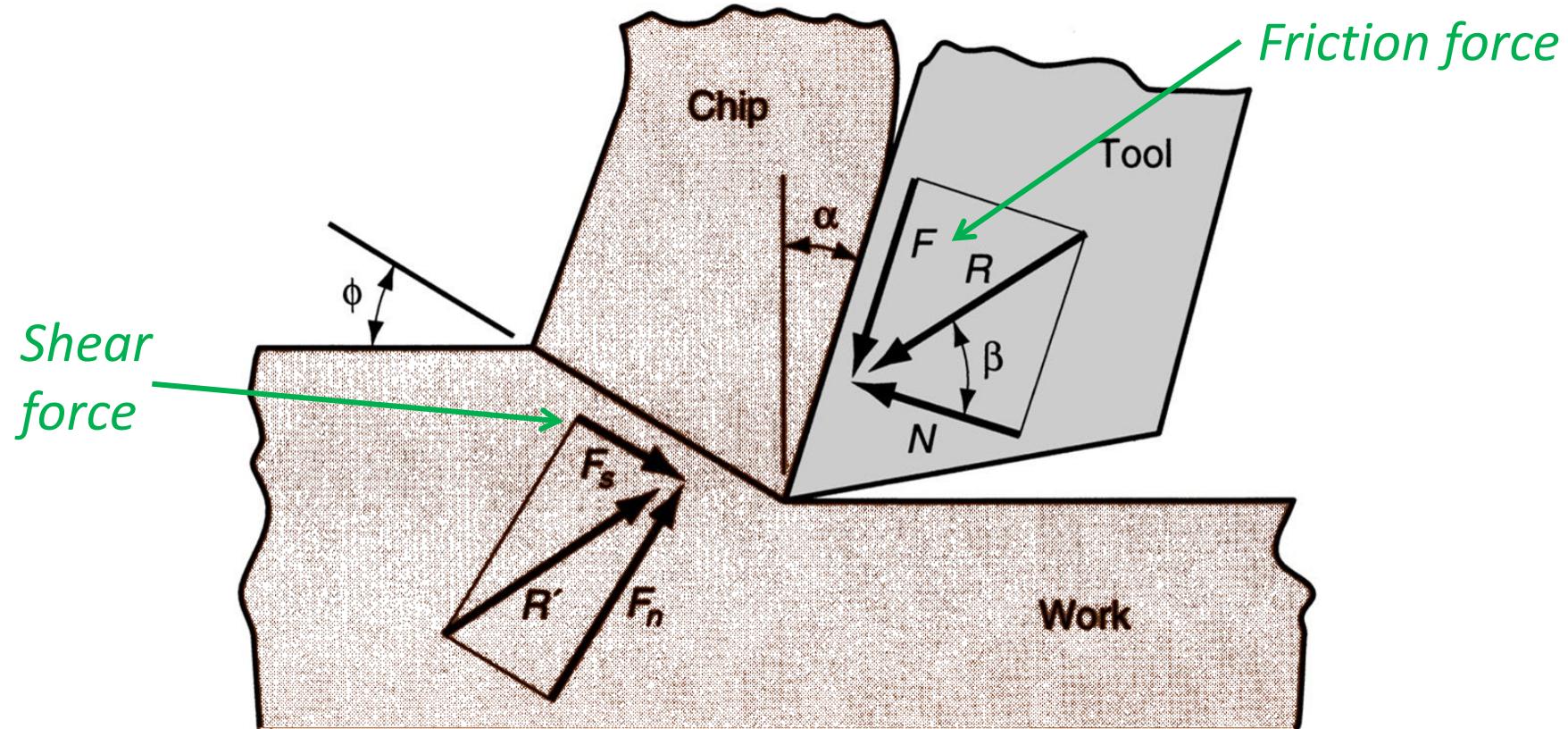
# Key parameters: chip thickness ratio



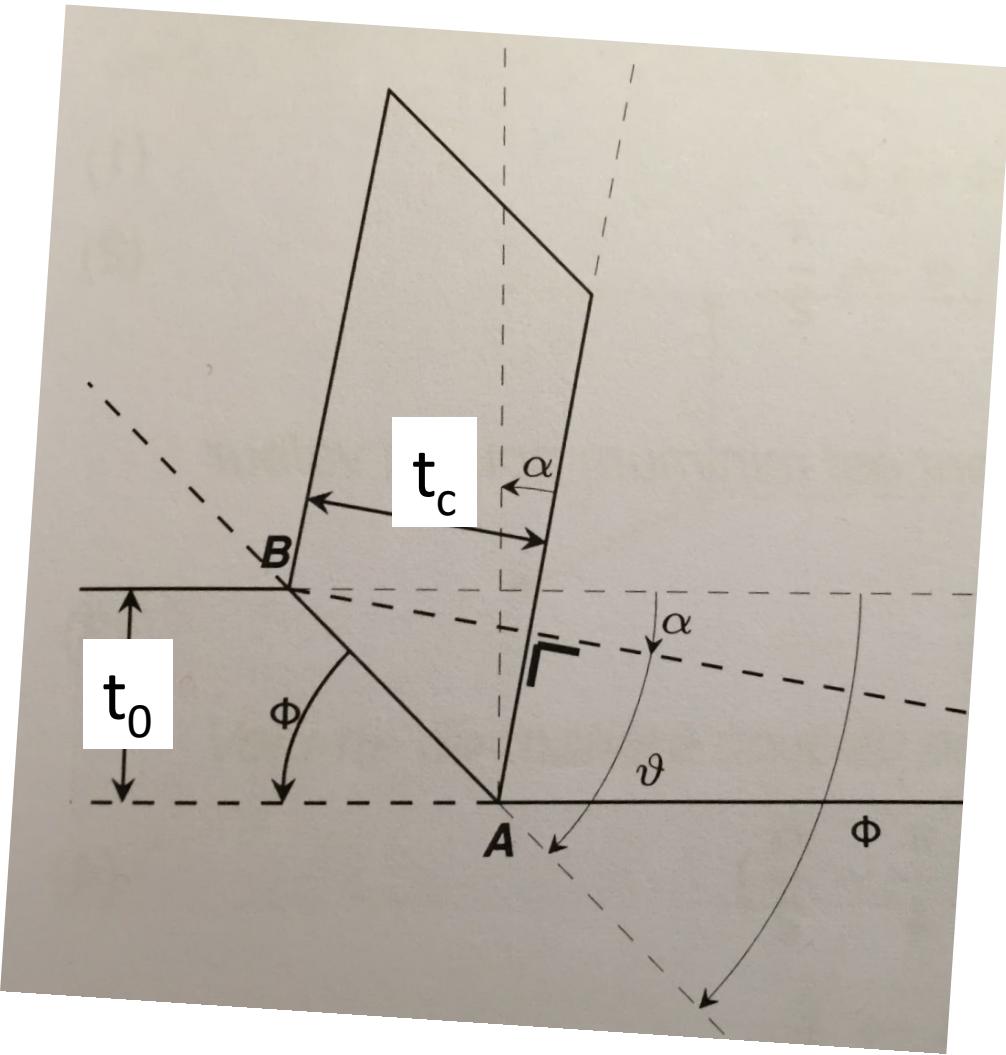
- Chip thickness after cut is always greater than before,  $r < 1.0$

# Forces acting during machining

- **Friction force  $F$  and Normal force to friction  $N$**
- **Shear force  $F_s$  and Normal force to shear  $F_n$**



# Chip thickness ratio vs definition angles



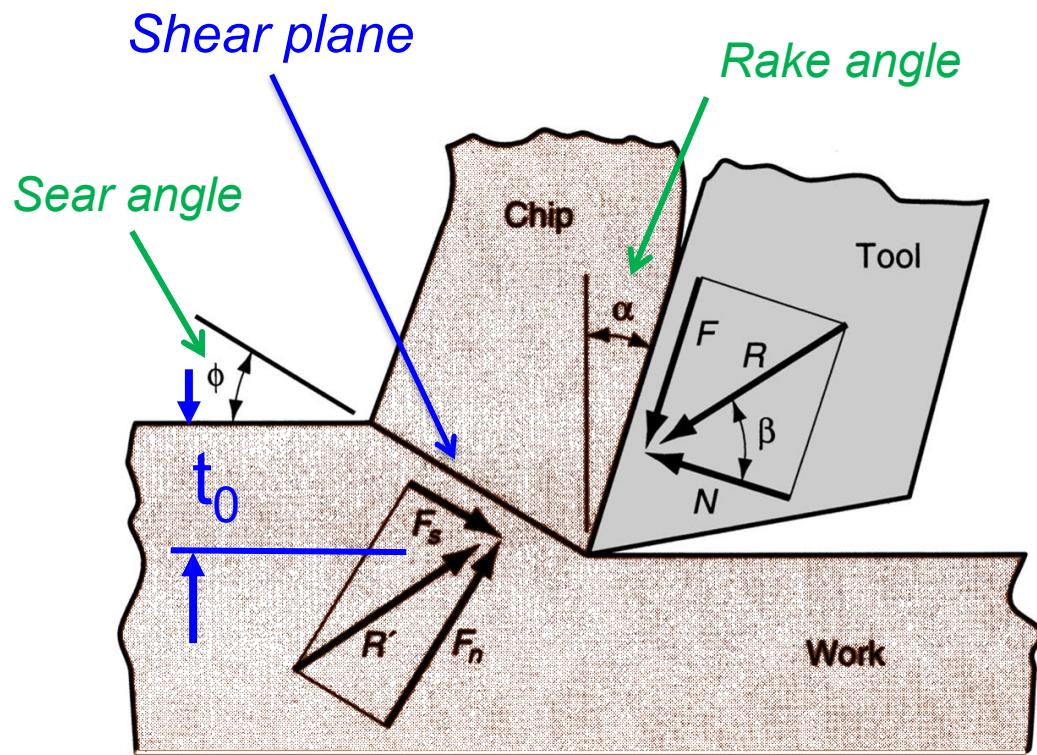
(Dessin E. Boillat)

$$t_0 = \|AB\| \sin \phi$$

$$t_c = \|AB\| \cos \vartheta$$

$$\frac{t_0}{t_c} = \frac{\sin \phi}{\cos \vartheta} = \frac{\sin \phi}{\cos(\phi - \alpha)}$$

# Shear plane approximation



**Shear stress** acting along the shear plane:  $\tau = \frac{F_s}{A_s}$

*Sheared surface*

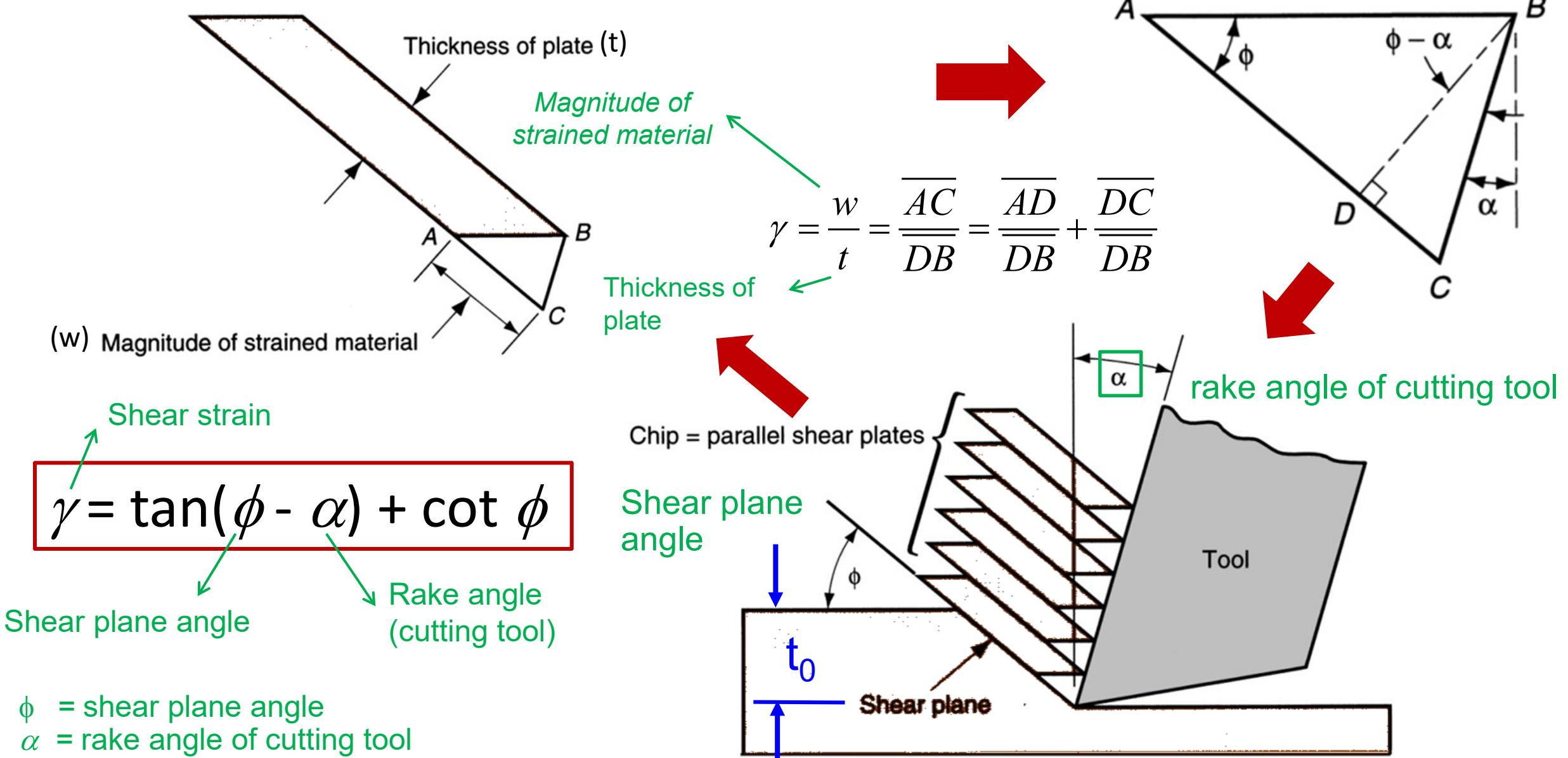
*Shear force*

$$\frac{F_s}{A_s}$$

*Cut depth*  $A_s = \frac{t_0 w}{\sin \phi}$  *Tool width*

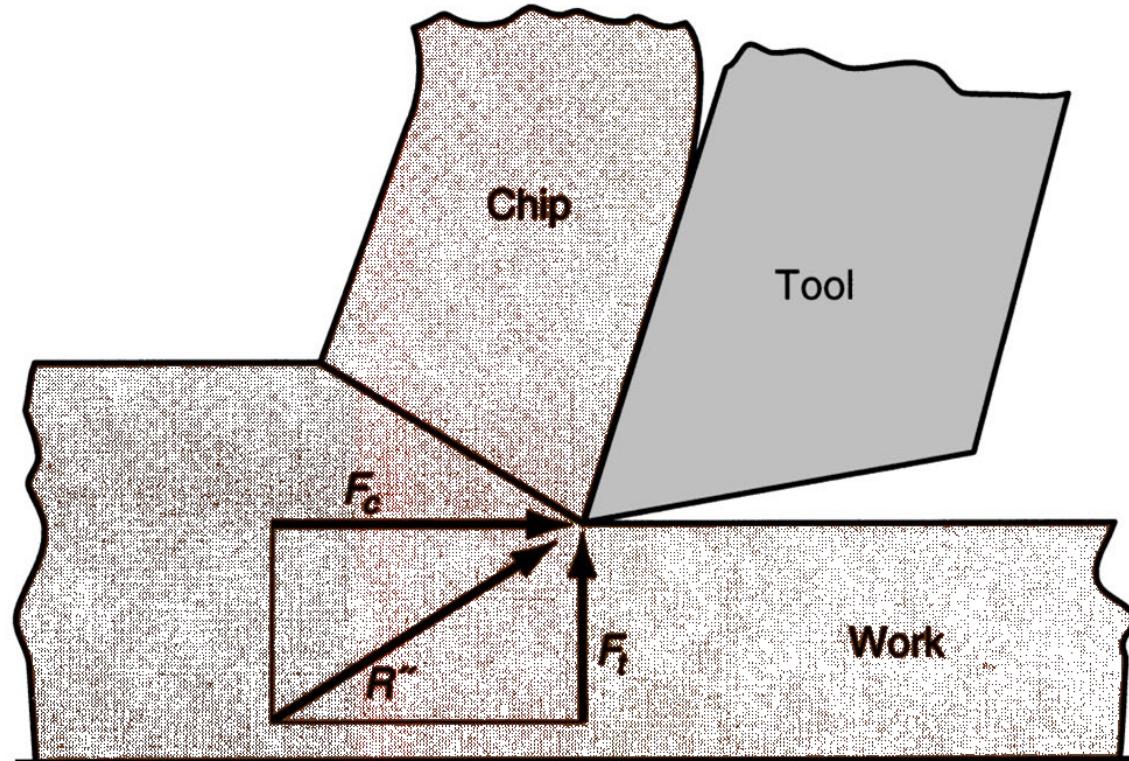
$$\tau = \frac{F_s}{\left( \frac{t_0 w}{\sin \phi} \right)}$$

# Pure shear strain model (approximation)



# Measurable forces during machining

- Forces  $F$ ,  $N$ ,  $F_s$ , and  $F_n$  cannot be directly measured
- Forces acting on the tool that can be measured: *Cutting force  $F_c$*  and *Thrust force  $F_t$*



# Forces in Metal Cutting derived from measurable forces

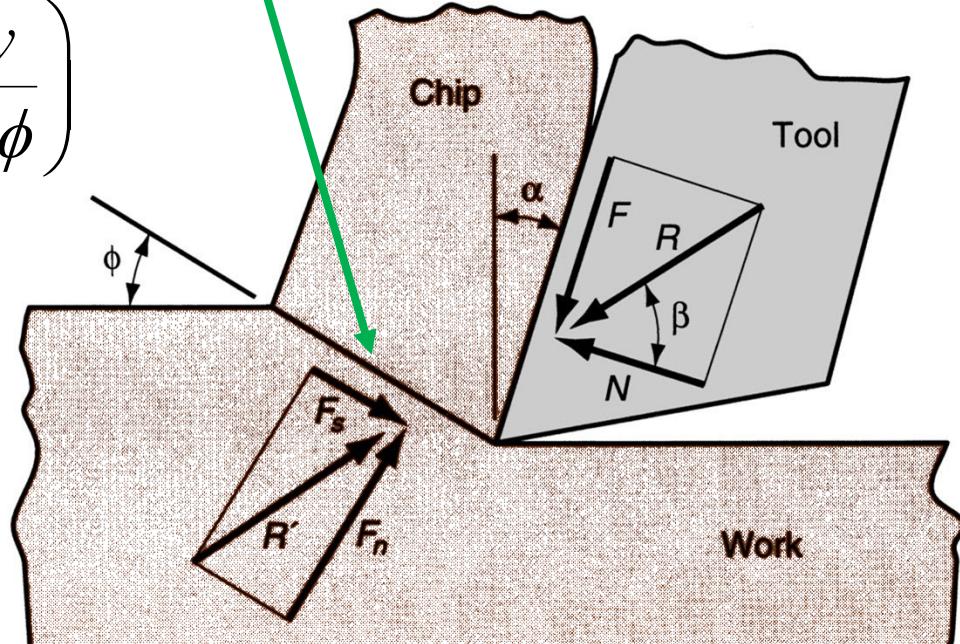
Friction force

$$F = F_c \sin \alpha + F_t \cos \alpha$$

Shear force

$$F_s = F_c \cos \phi - F_t \sin \phi$$

$$\tau = \frac{F_s}{\left( \frac{t_0 w}{\sin \phi} \right)}$$



Normal to  
the tool

$$/ \quad N = F_c \cos \alpha - F_t \sin \alpha$$

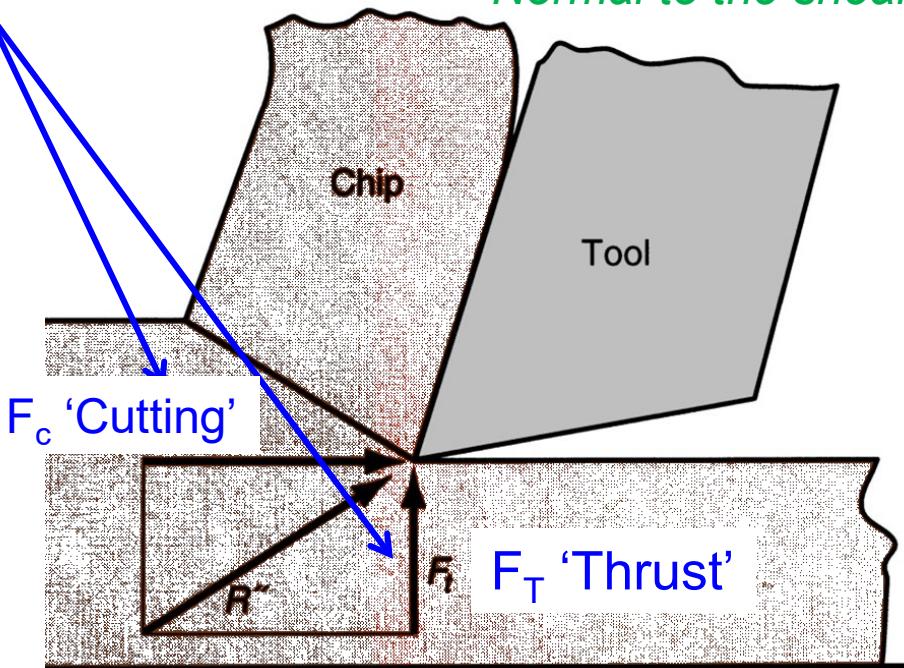
$$/ \quad F_n = F_c \sin \phi + F_t \cos \phi$$

Rake angle

Shear angle

Normal to the shear plane

Are measurable !



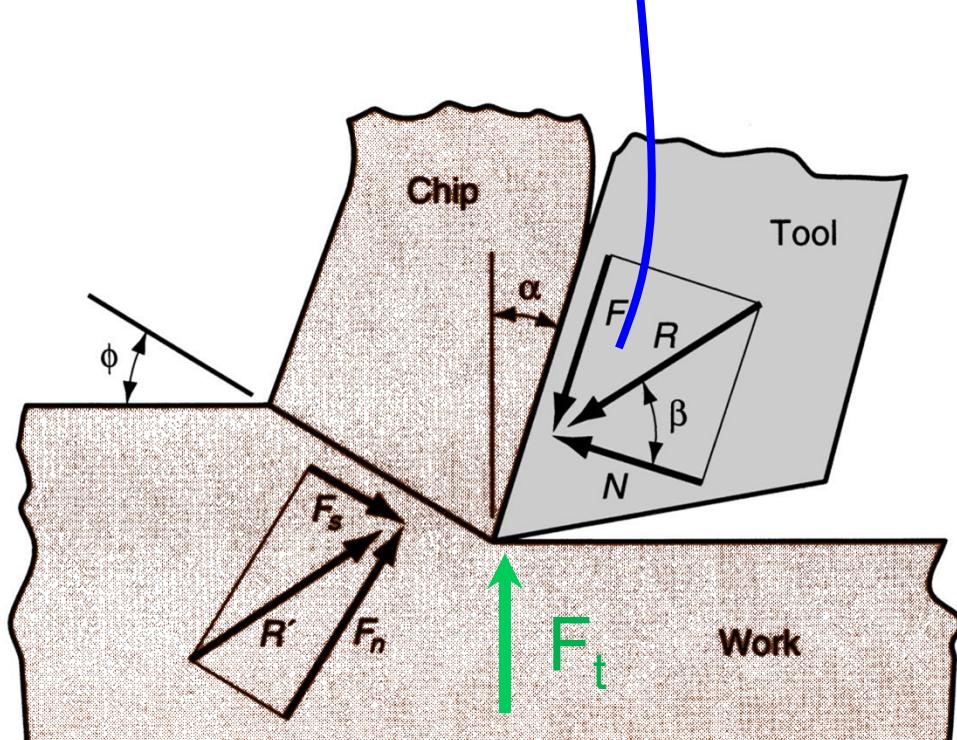
# Expressing the Thrust ( $F_t$ ) as a function of friction

Coefficient of friction between tool and chip:

$$\mu = \frac{F}{N} \quad \text{with}$$

$$\mu = \tan \beta \quad (\beta = \arctan \mu)$$

*'Friction angle'*



We have:

$$F_t = \| \mathbf{R} \| \cos(\alpha - \beta)$$

Exists if

$$F_t > 0 \Leftrightarrow (\alpha - \beta) < \frac{\pi}{2}$$

# $F_s$ and $F_t$ as a function of shear strength only...

$$F_s = \tau A_s$$

$$F_c = F_s \cos(\beta - \alpha) / [\cos(\phi + \beta - \alpha)]$$

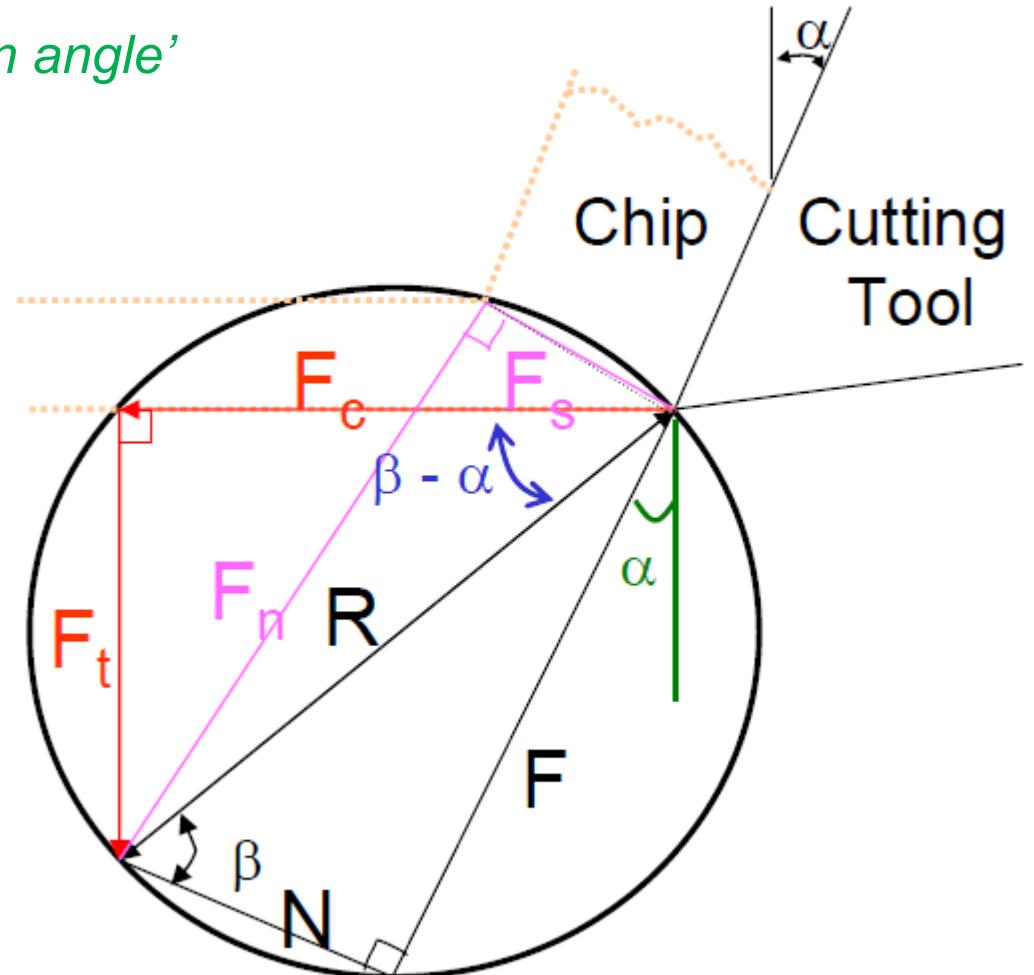
$$F_t = F_s \sin(\beta - \alpha) / [\cos(\phi + \beta - \alpha)]$$

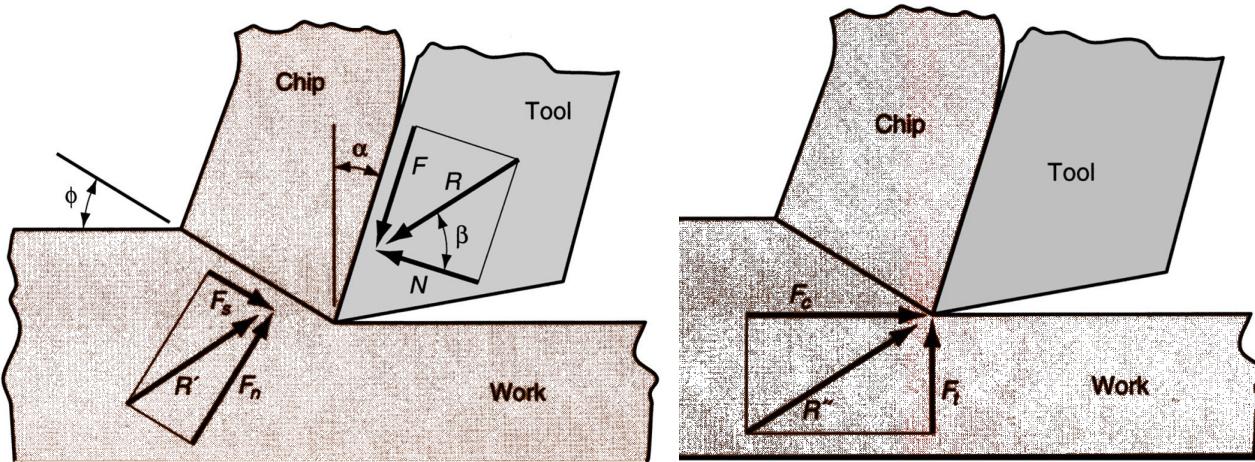
'Shear angle'

'Friction angle'

'Rake angle'

We use the equations from slide 36, and express  $F_c$  and  $F_t$  only as a function of the shear force and the shear strength and the friction angle. It is essentially a geometrical problem that can be solved by reporting all the forces on the same diagram (left).





## The Merchant condition

Merchant Equation: 
$$\tau = \frac{F_c \cos \phi - F_t \sin \phi}{\left( \frac{t_0 w}{\sin \phi} \right)}$$

(combining slide 33 and slide 36)

- Minimizing shear stress
- Using  $F_c$  and  $F_t$  as a function of the shear strength (previous slide)
- The shear plane angle  $\phi$  minimizes the energy when:

$$\phi = \frac{\pi}{4} + \frac{(\alpha - \beta)}{2}$$

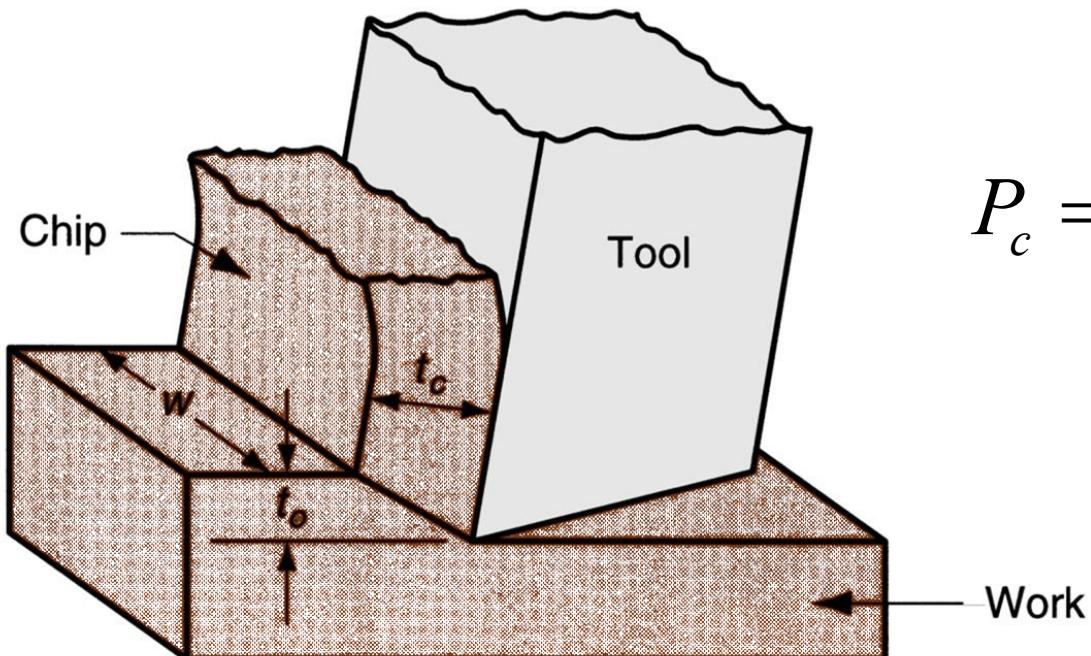
$$\beta = \text{arctg}(\mu)$$

- *Hypothesis: 'The shear angle adjusts itself to minimize the cutting force'  $\Leftrightarrow$  'The shear plane is a plane of maximum shear stress'*

**Conclusion:** Knowing the friction coefficient, one can apply the optimal rake angle ( $\alpha$ )

# Energy considerations

- Power of a force:  $P = F v$  (unit W)
- Here, the power to perform machining is:  $P_c = F_c v$



$$P_c = vF_c = 2\tau \left[ \frac{\cos(\alpha - \beta)}{1 + \sin(\alpha - \beta)} \right] (t_0 w) v$$

*(for Merchant's conditions)*

# Specific cutting energy

- We define the cutting rate as:

$$\mu = \tan \beta$$

$$(\beta = \arctan \mu)$$

$$\dot{V}_c = v(t_0 w)$$

in (mm<sup>3</sup>/s)

Cutting rate [mm<sup>3</sup>/s]

Feed rate

Chip section

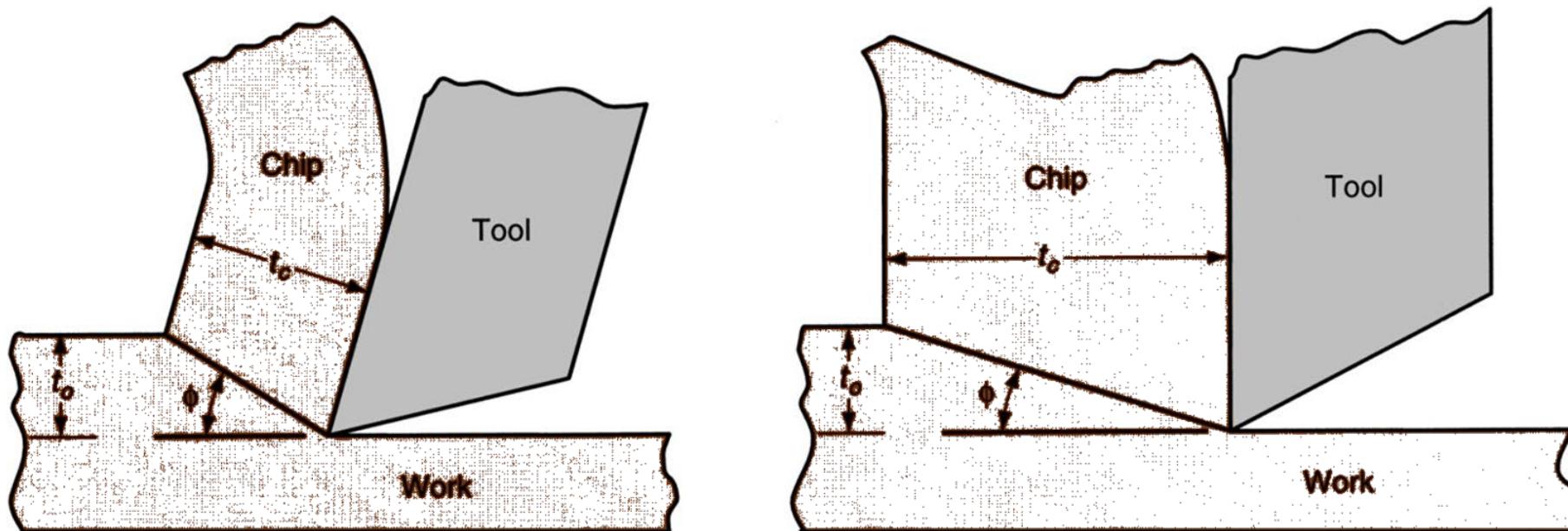
$$P_c = v F_c = 2\tau \left[ \frac{\cos(\alpha - \beta)}{1 + \sin(\alpha - \beta)} \right] \dot{V}_c$$

Specific cutting energy ( $e_c$ ) [J/mm<sup>3</sup>]

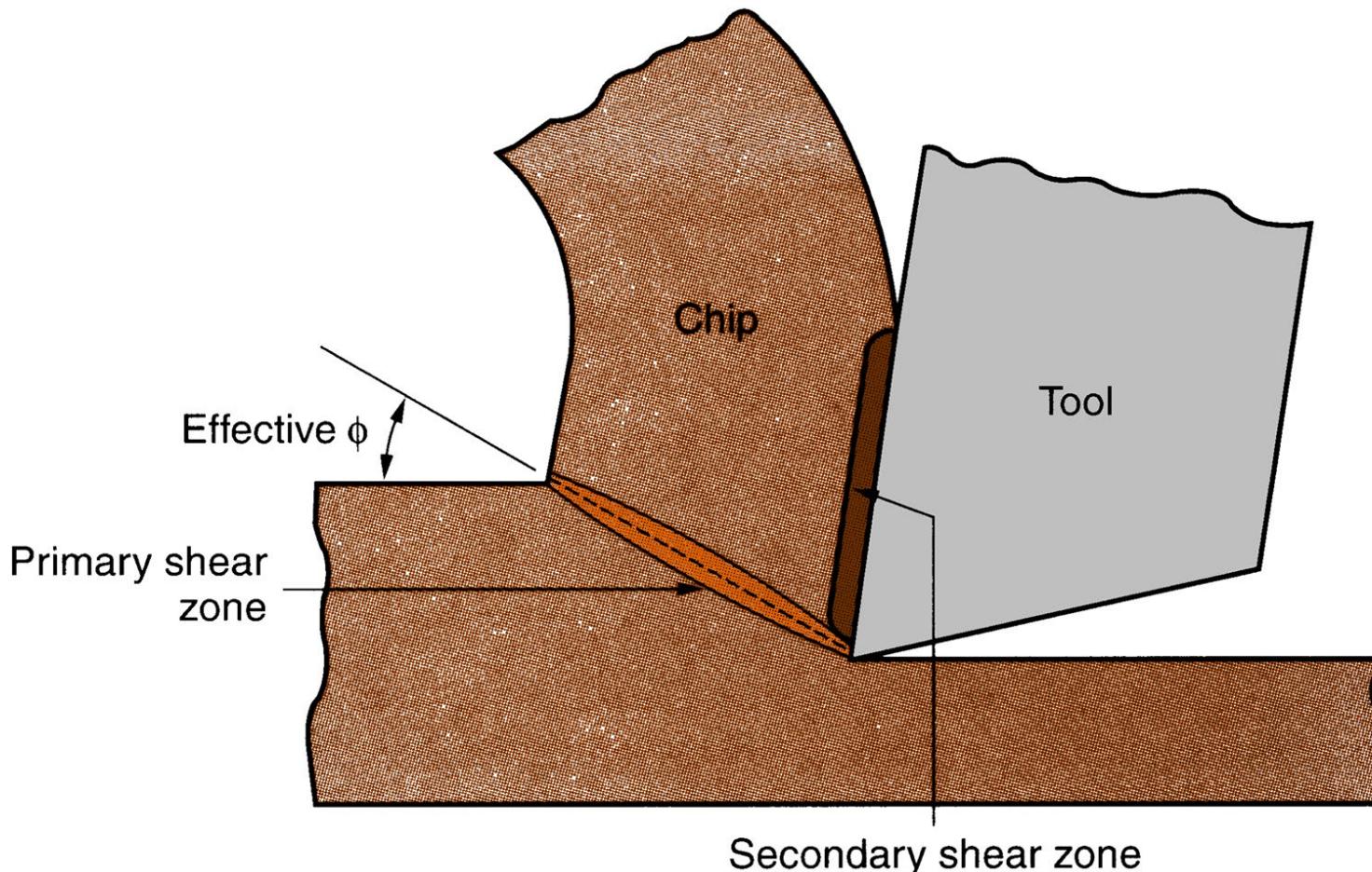
Cutting rate [mm<sup>3</sup>/s]

# Discussion / existence of an **optimal** tool-cutting angle

- Increase in friction angle  $\Leftrightarrow$  decreases of shear angle
- Higher shear plane angle  $\Leftrightarrow$  smaller shear plane  $\Leftrightarrow$  lower shear force
- Consequences: lower cutting forces, power, temperature, ...  $\Rightarrow$  easier machining, but tool angle needs to satisfy the Merchant condition

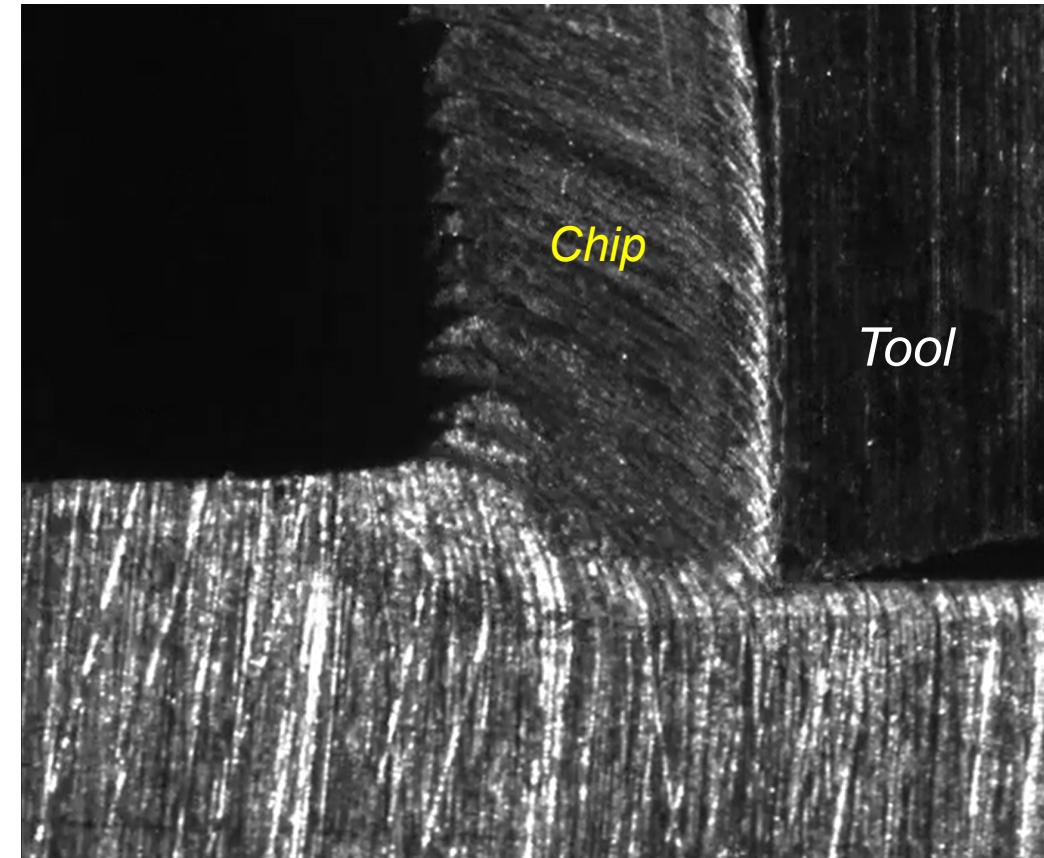
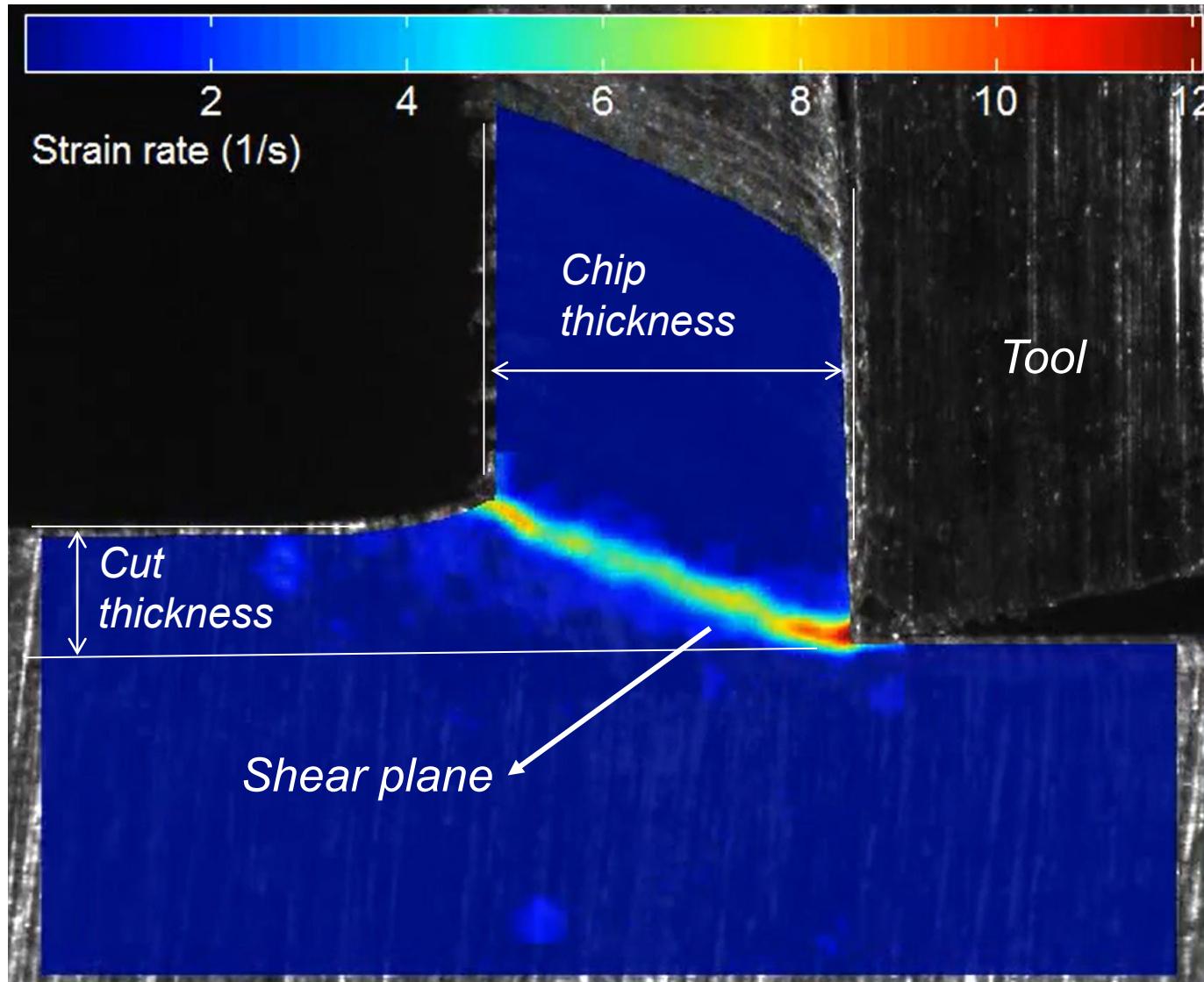


# A more realistic description...



*Presence of a secondary shear zone*

# Continuous chip formation (real case illustration)



<https://youtu.be/xmOyaYEWbT4?si=k2xh0T6BpCO05E3L>

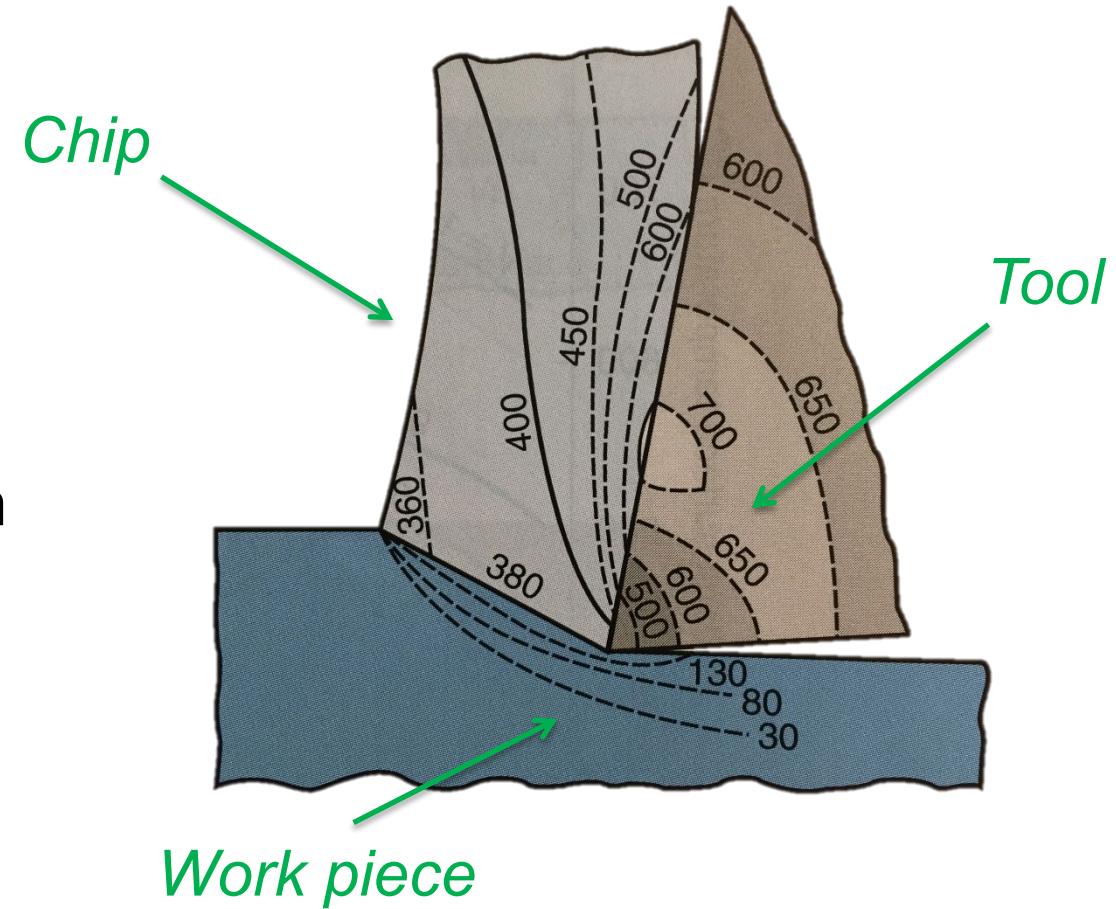
# Specific cutting energy: typical order of magnitude

Material	Specific energy*	
	W-s/mm <sup>3</sup>	hp-min/in <sup>3</sup>
Aluminum alloys	0.4–1.1	0.15–0.4
Cast irons	1.6–5.5	0.6–2.0
Copper alloys	1.4–3.3	0.5–1.2
High-temperature alloys	3.3–8.5	1.2–3.1
Magnesium alloys	0.4–0.6	0.15–0.2
Nickel alloys	4.9–6.8	1.8–2.5
Refractory alloys	3.8–9.6	1.1–3.5
Stainless steels	3.0–5.2	1.1–1.9
Steels	2.7–9.3	1.0–3.4
Titanium alloys	3.0–4.1	1.1–1.5

\*At drive motor, corrected for 80% efficiency; multiply the energy by 1.25 for dull tools.

# Temperature / Heat transfer

- About **98%** of the energy in machining is converted into heat...
- Most of the energy goes in the tool and in the chip
- Temperatures can be very high at the tool-chip
- The remaining energy (about **2%**) is retained as elastic energy in the chip
- **Consequences:** requires coolant during operation ...



# Cutting Temperature

- Experimental methods can be used to measure temperatures in machining (tool-chip thermocouples, IR camera, etc.)
- K. Trigger's empirical law: determined the speed-temperature relationship to be of the form:

$$T = Kv^m$$

The diagram illustrates the empirical law for cutting temperature. At the top center is the equation  $T = Kv^m$ . Four green arrows point from the text labels below to the variables in the equation: 'Temperature' points to  $T$ , 'Cutting speed' points to  $v$ , 'Thermal conductivity of the work material' points to  $K$ , and 'Empirical factor (m)' points to  $m$ .

Temperature

Cutting speed

Thermal conductivity of the work material

Empirical factor (m)

# Cutting Temperature: other models...

- Several analytical methods to calculate cutting temperature
- Example. N. Cook derived from dimensional analysis using experimental data for various work materials

$$T = 0.4 \left( \frac{e_c}{\rho C_p} \right) \left( \frac{vt_o}{K} \right)^{1/3}$$
$$e_c = 2\tau \left[ \frac{\cos(\alpha - \beta)}{1 + \sin(\alpha - \beta)} \right]$$

*Cutting speed*

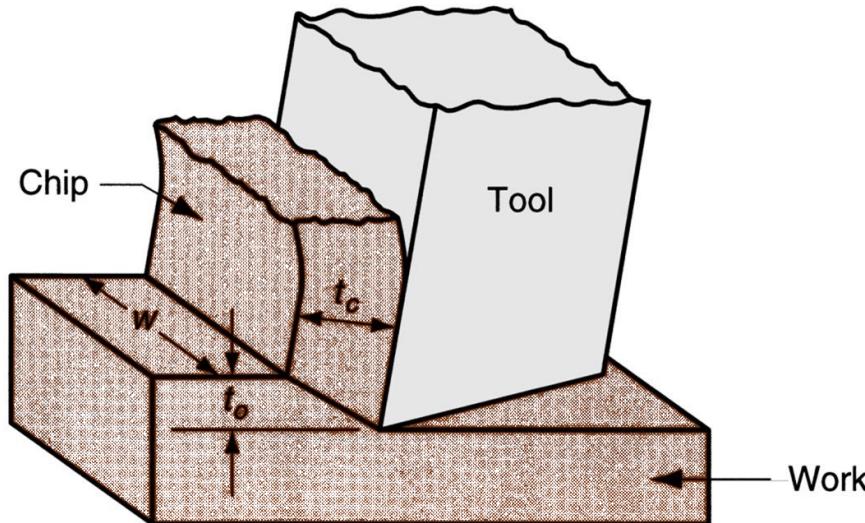
*Cutting thickness*

*Thermal conductivity of the material*

*Calorific capacity*

*Material density*

# Cutting tools wear: empirical model (Taylor)



Material	n
High-speed steels	0.08 – 0.2
Carbides	0.2 – 0.5
Ceramics	0.5 – 0.7

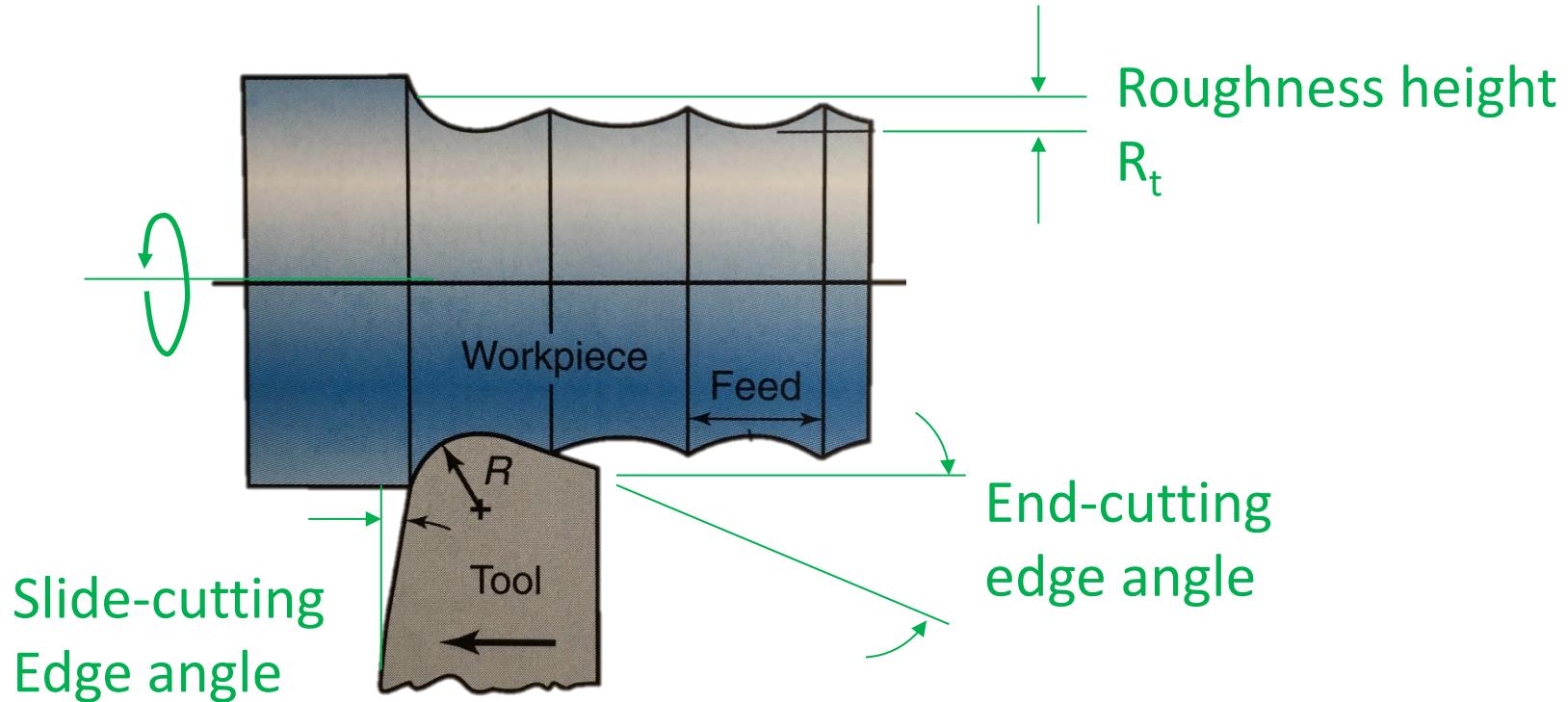
$$LT = \left( \frac{C}{w^x t_0^y v} \right)^{\frac{1}{n}}$$

Annotations for the equation:

- Life time (LT)* points to the leftmost term  $LT$ .
- Tool width* points to the term  $w^x$ .
- Penetration depth* points to the term  $t_0^y$ .
- Cutting speed* points to the term  $v$ .
- Constant* points to the term  $C$ .

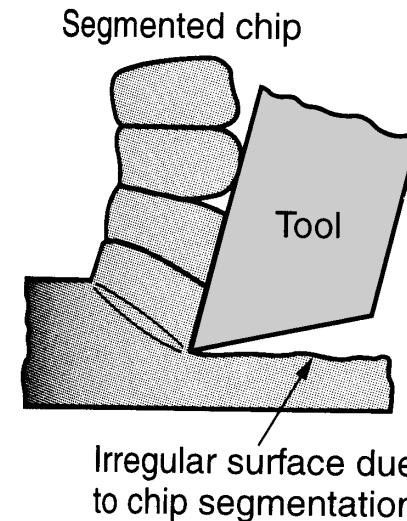
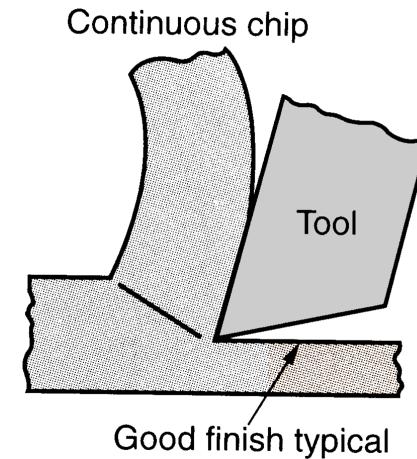
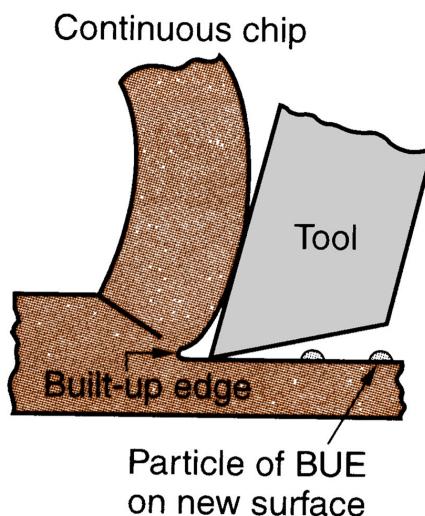
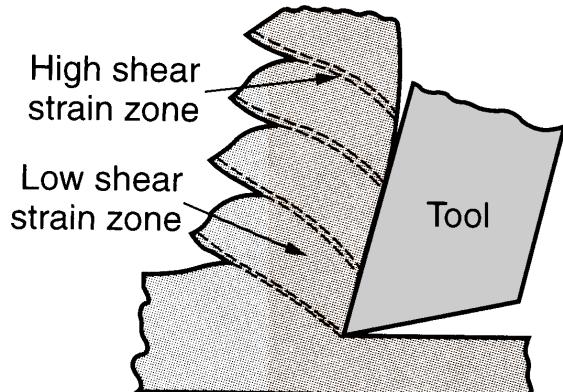
$n, x, y$  : experimental parameters

# Effect of tool wear on surface finish...



# The produced chip tells about machining parameters...

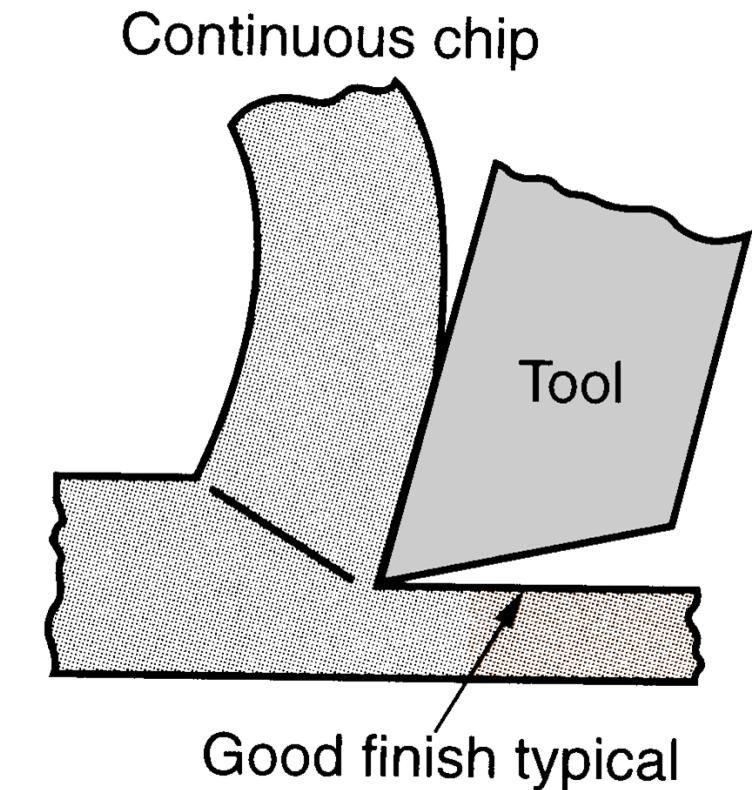
1. Continuous chip
2. Segmented chip
3. Continuous chip with Built-up Edge (BUE)
4. Saw-tooth appearance



Check illustrative  
videos on the Moodle!

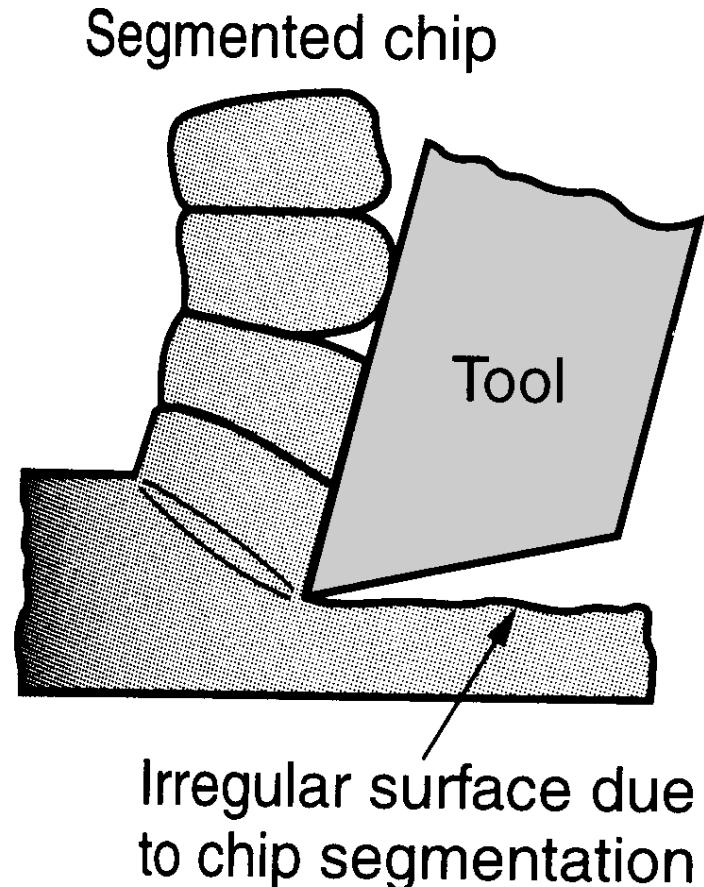
# Ideal case: continuous chip formation

- **Ductile work materials** (e.g., low carbon steel)
- High cutting speeds
- Small feeds and depths
- Sharp cutting edge on the tool
- Low tool-chip friction



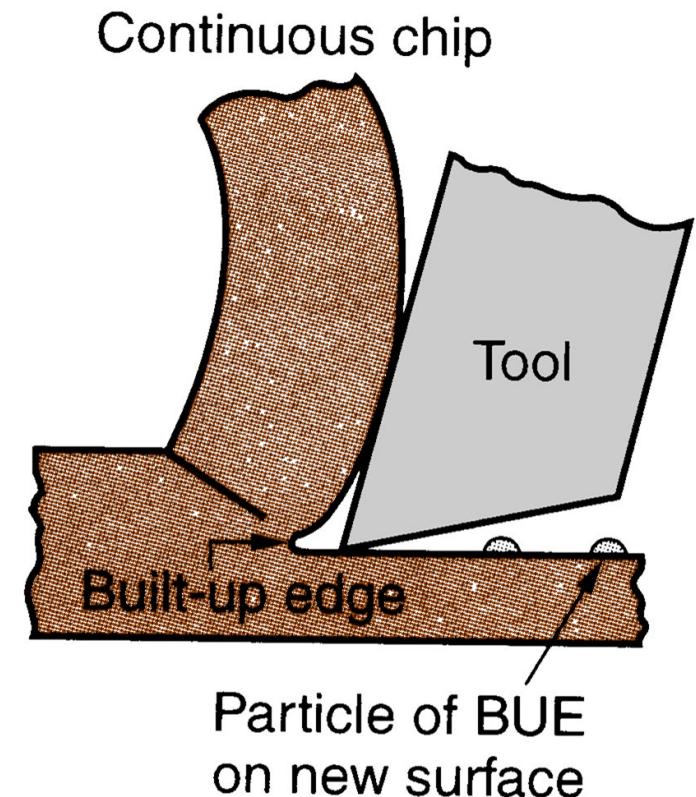
# Segmented chip...

- **Brittle work materials** (e.g., cast irons)
- Low cutting speeds
- Large feed and depth of cut
- High tool-chip friction



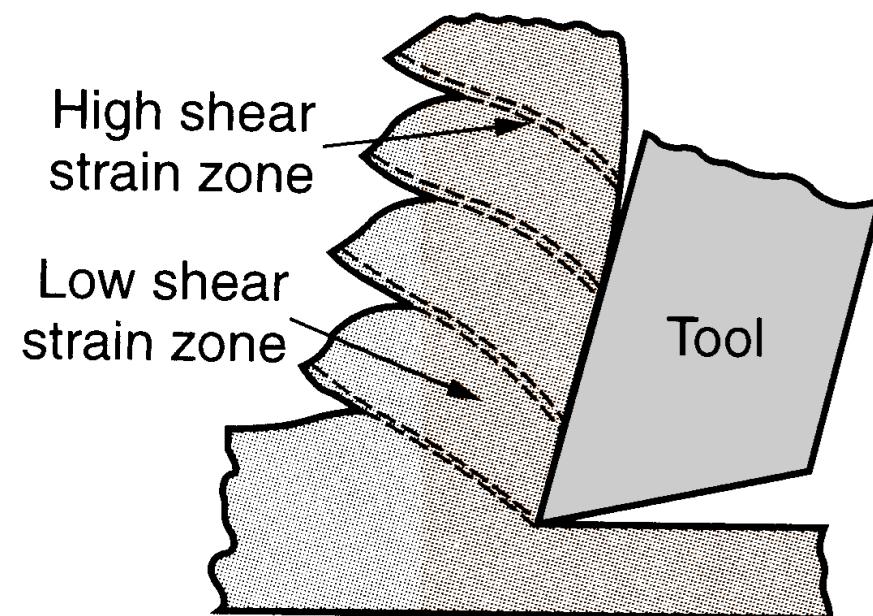
# Continuous chip with built-up edge (BUE)

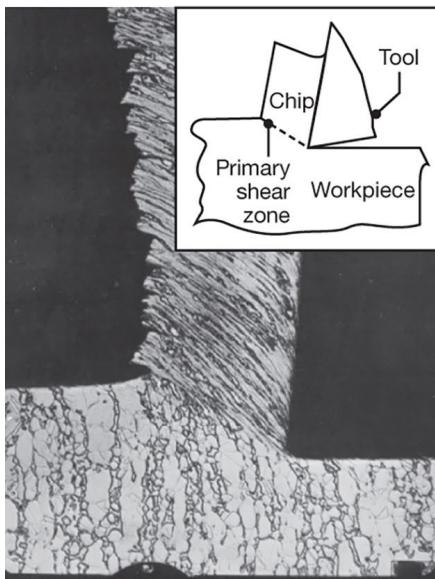
- **Ductile materials**
- Low-to-medium cutting speeds
- Tool-chip friction causes portions of chip to adhere to rake face
- BUE formation is cyclical; it forms, then breaks off



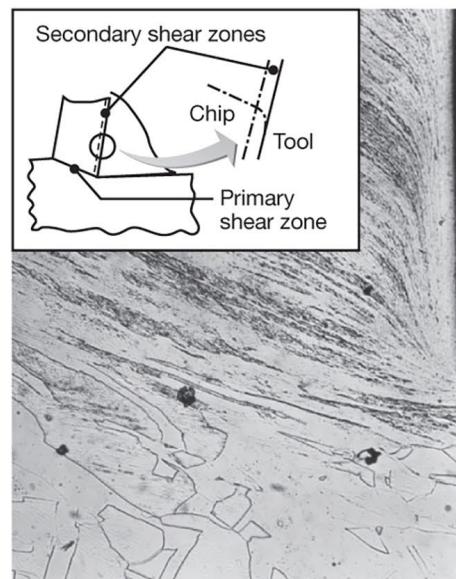
# Saw-tooth appearance

- Semi-continuous - saw-tooth appearance
- Cyclical chip formation of alternating high shear strain then low shear strain
- Associated with difficult-to-machine metals at high cutting speeds

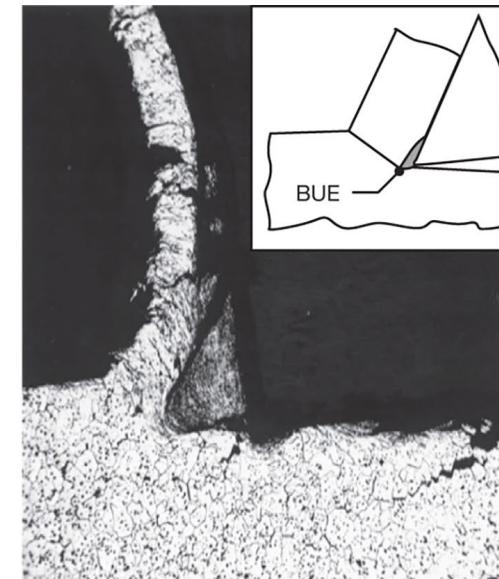




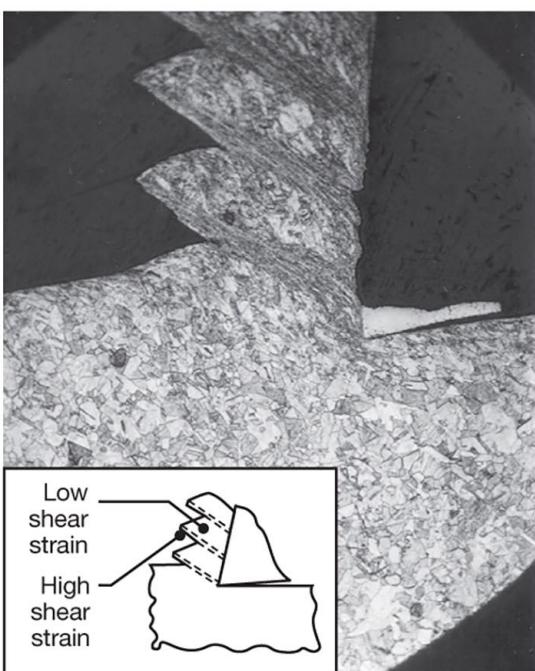
(a)



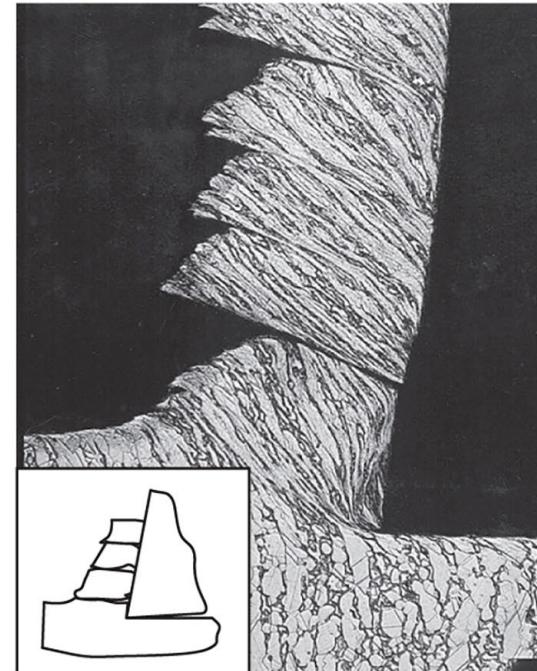
(b)



(c)

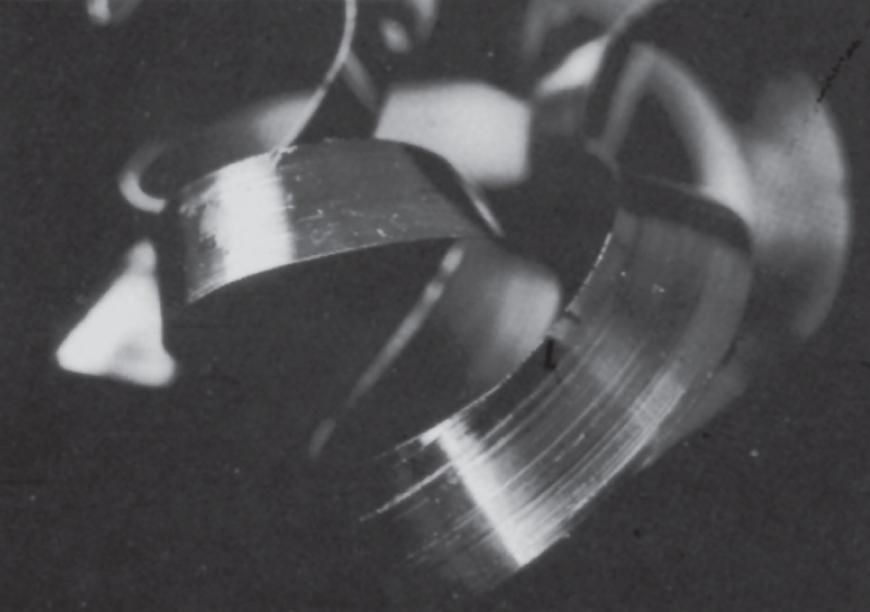


(d)

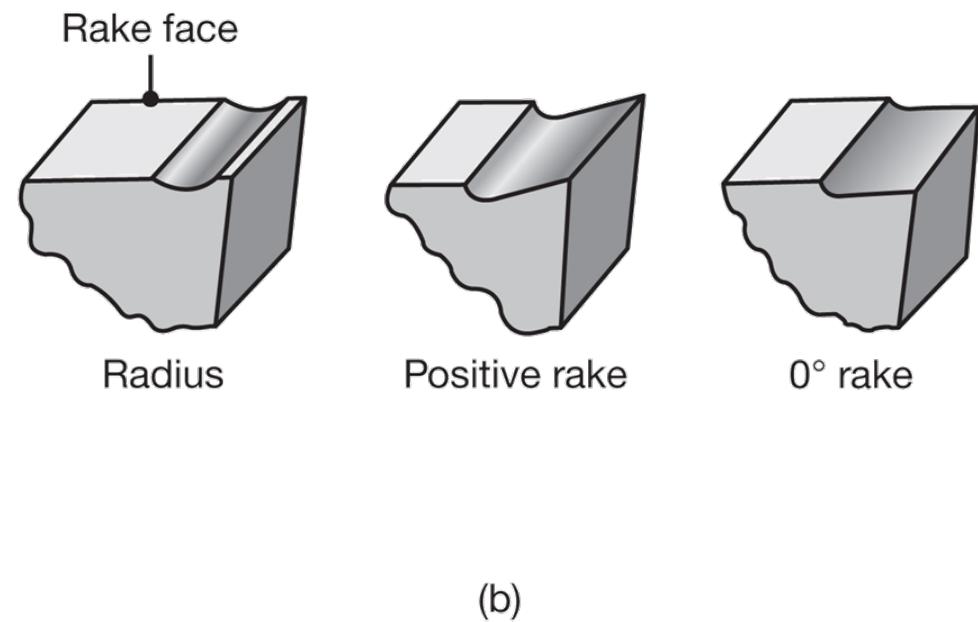
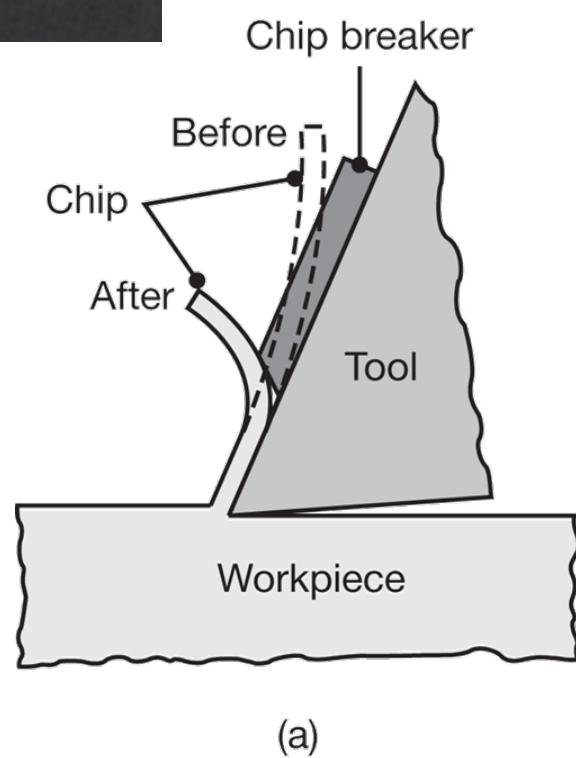


(e)

Type of chips...

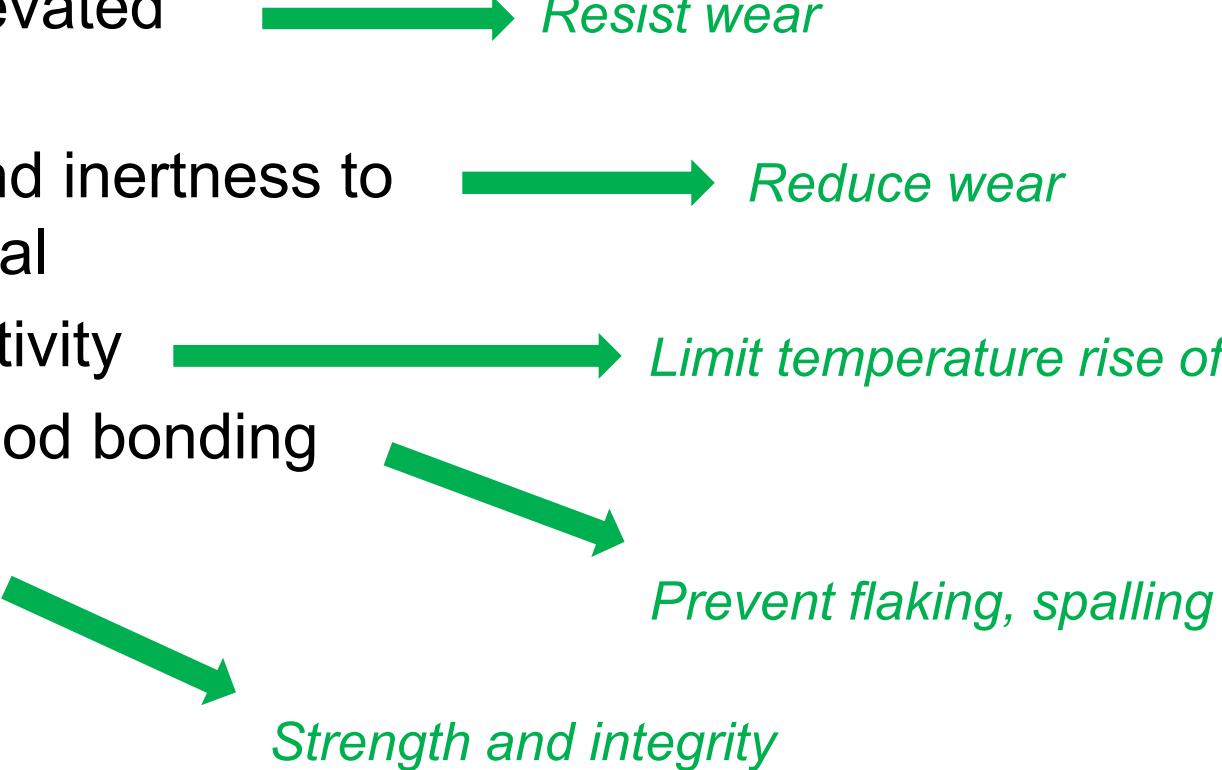


## Some technological aspects... (chip breaker)



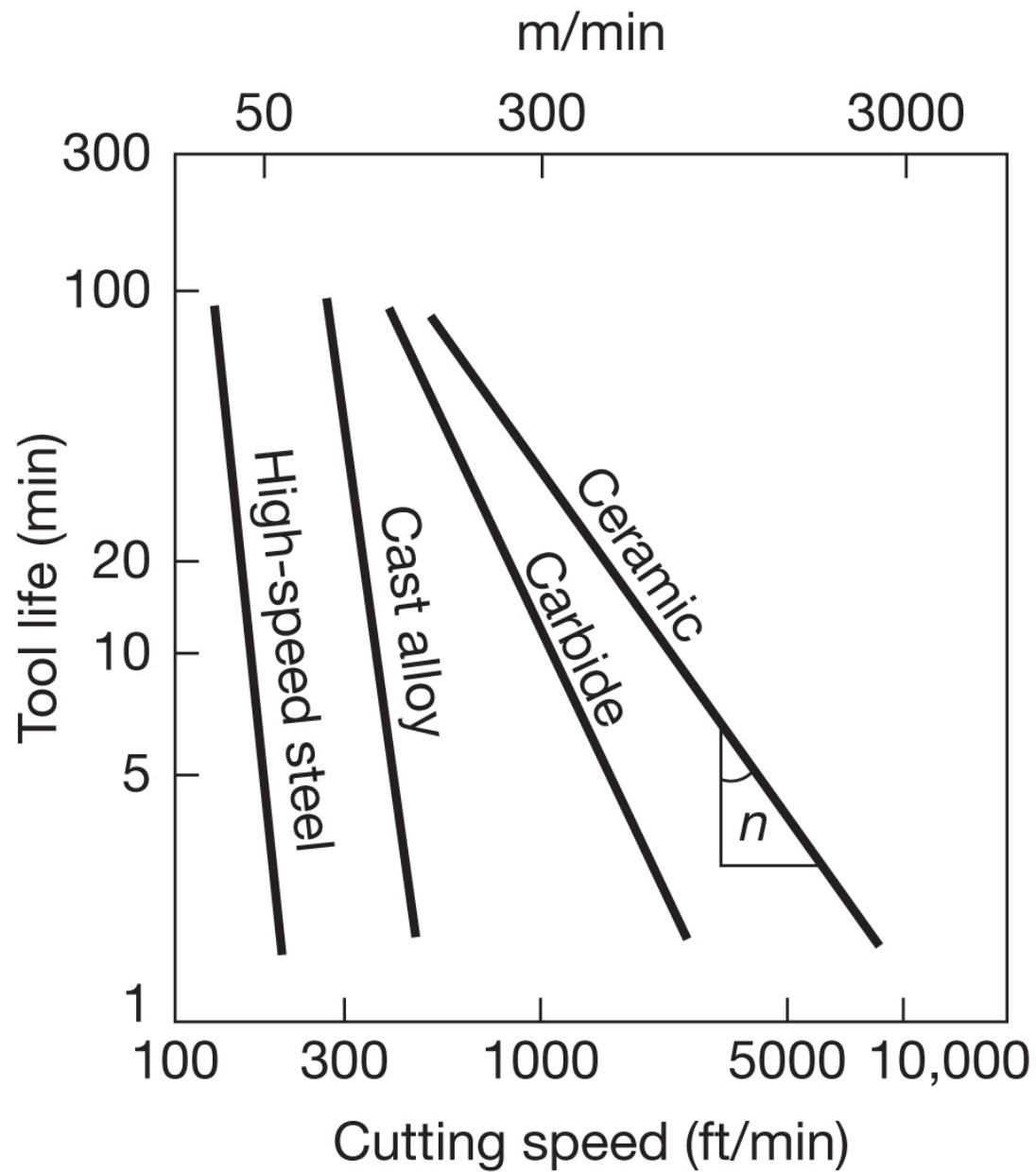
# Importance of tool coatings and materials

- High hardness at elevated temperature  *Resist wear*
- Chemical stability and inertness to the workshop material  *Reduce wear*
- Low thermal conductivity  *Limit temperature rise of the substrate*
- Compatibility and good bonding
- Little or no porosity



*Strength and integrity*

*Prevent flaking, spalling*



Example of tool-life curves for selected cutting tool materials as a function of the cutting-speed

# Progress made in cutting speed thanks to the tooling...

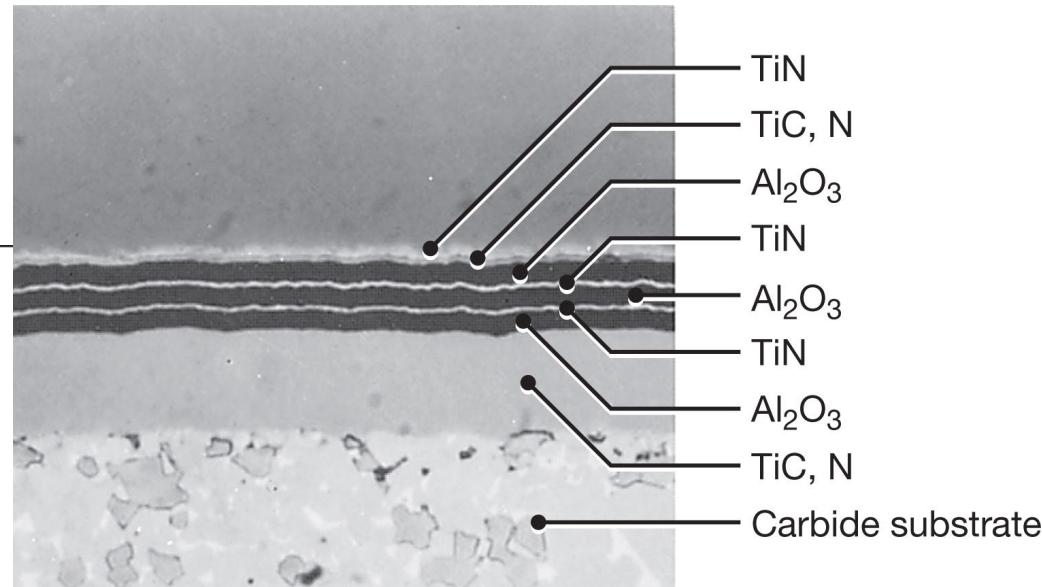
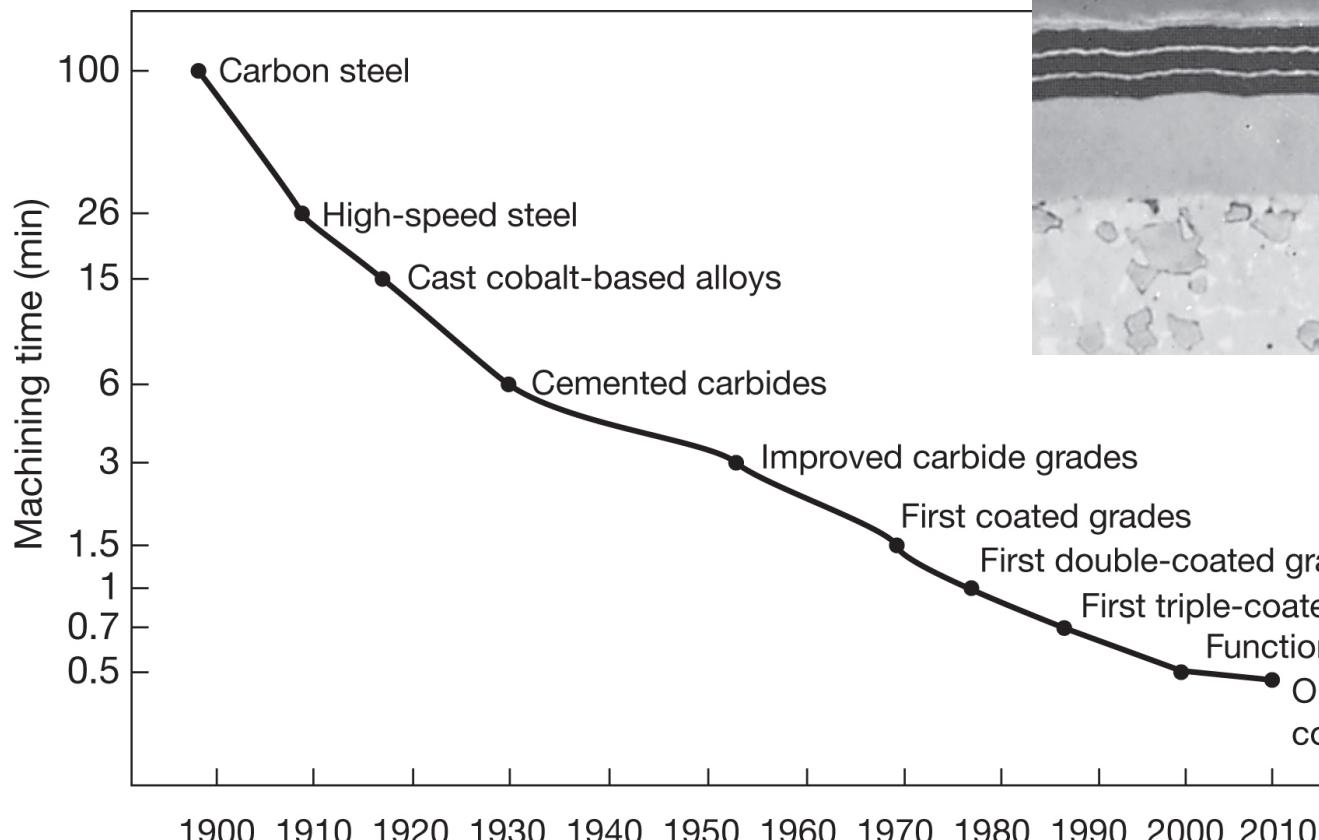
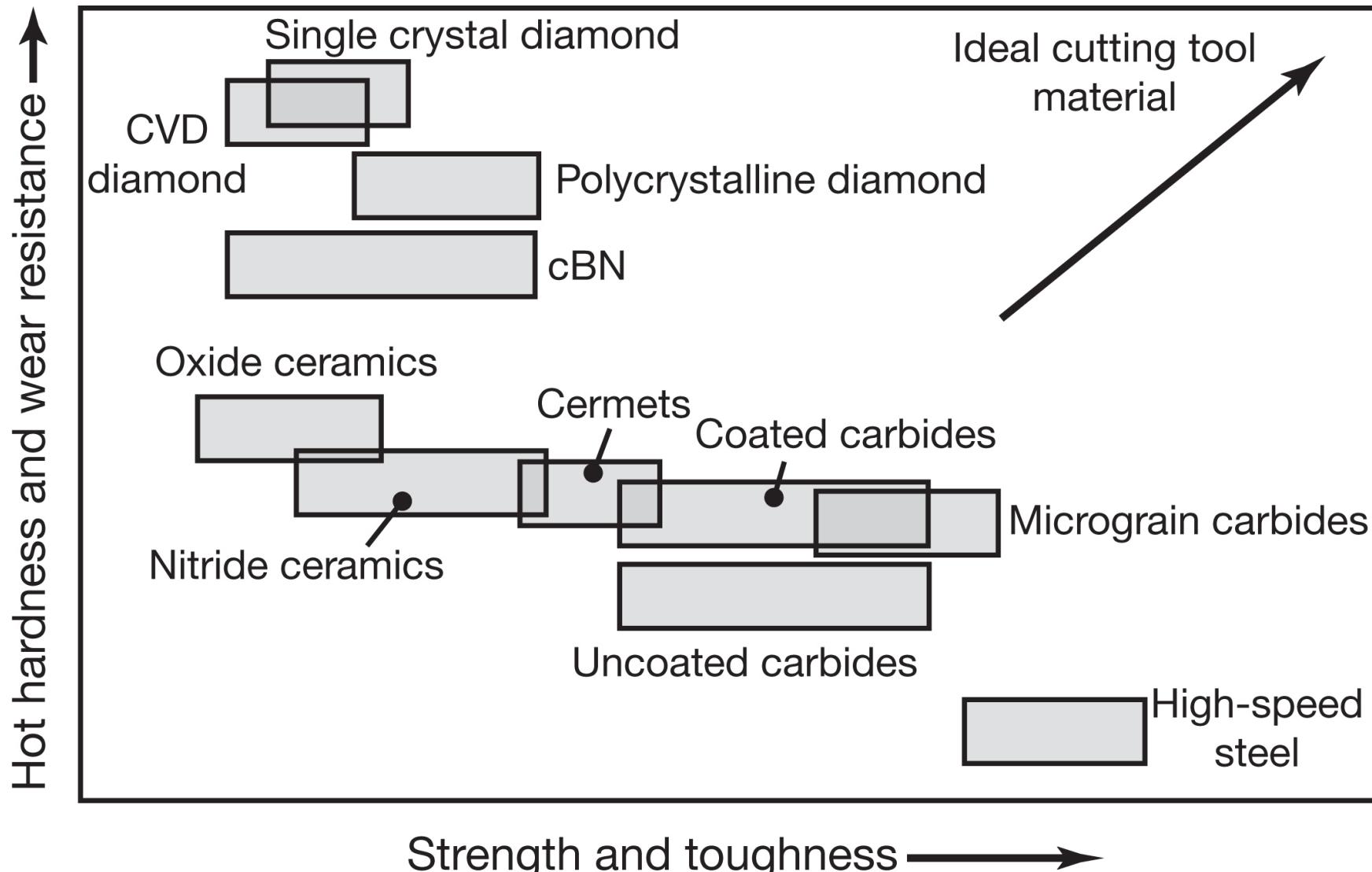


Illustration Kennametal, Inc.

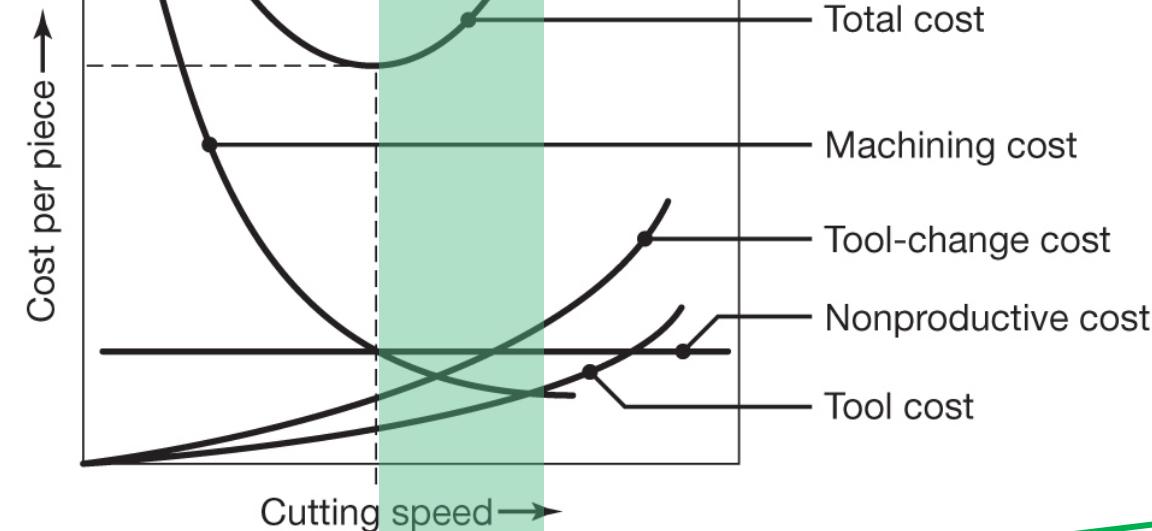


(source Sandvik Coromant)

# Range of properties for cutting tools

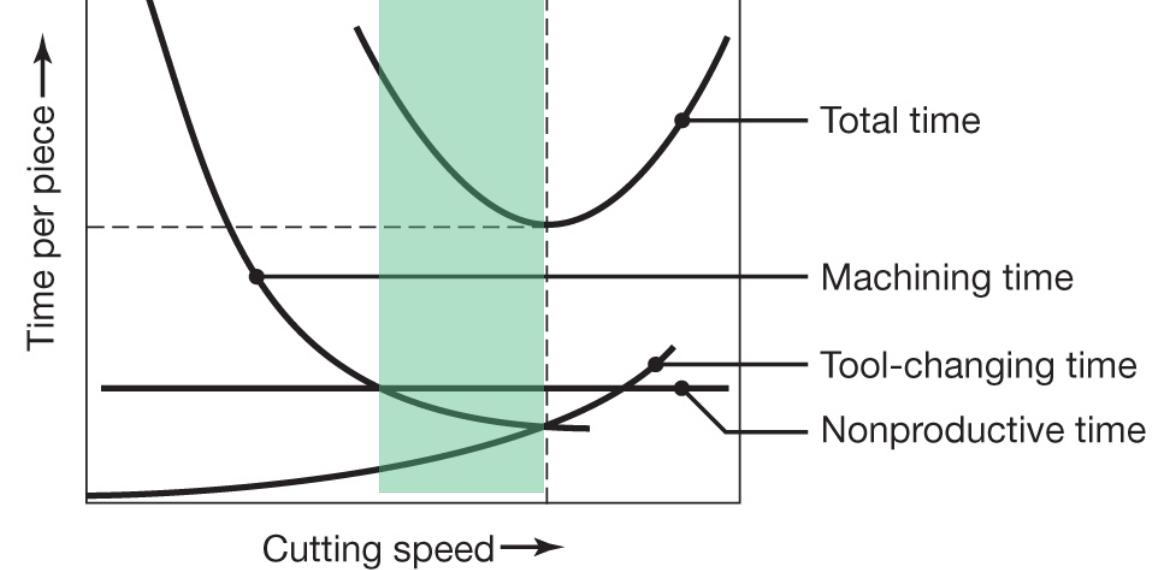


# Economics



Production cost

Optimal zone  
(High efficiency machining at optimal cost)



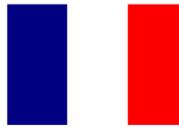
Production time

# Roughing vs. Finishing

- Production is usually done in multiple steps... First **roughing**, then **finishing**.
- **Roughing** - removes large amounts of material from the initial workpiece
  - Creates shape approaching the desired geometry, but leaves some material for finish cutting
  - Done at high feeds and depths, low speeds
- **Finishing** – Final part geometry
  - Achieves final dimensions, tolerances, and finish
  - Done at Low feeds rate and depths, high cutting speeds

# Key points to remember

- A general view of conventional machining methods
- The physical principles behind material removal by mechanical cutting and to calculate the key parameters
- Basic equations to estimate material removal rates (MRR)
- Importance of tooling
- Economical aspects: the optimization between tool costs and machining speed.



- Machining by material removal: *Usinage par enlèvement de matières*
- Cutting: *Découpage* / Cutting-tool: *Outil de coupe*
- Milling: *Fraisage* / End-mill: *Fraise*
- Drilling: *Précage* / Drill: *Forêt*
- Turning: *Tournage*
- Threading: *Taraudage*
- Chip: *Copeau*
- Rake: *Copeau*
- Reaming: *Alésage*
- Knurling: *Moletage*
- Roughing: *Usinage grossier*
- Finishing: *Usinage de finition*
- Saw-tooth: *Dent de scie*
- Feed rate: *Vitesse d'avance de l'outil*
- Rake: *'rateau'*
- Flank face: *Flanc de l'outil*

## Credits (sketches & Illustrations)

**Unless stated otherwise:** illustrations are adapted from: Manufacturing Engineering & Technology, M.C. Shaw, P.K. Wright, S. Kalpakjian, Pearson.